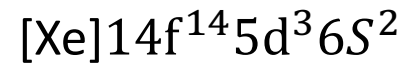


TaS₂

TaS2 Metal or insulator?

- Ta electronic configuration



Periodic table of the elements

group 1*																			18
1	2											13	14	15	16	17	18		
1	H																He		
2	3	4											5	6	7	8	9	10	
	Li	Be											B	C	N	O	F	Ne	
3	11	12											13	14	15	16	17	18	
	Na	Mg											Al	Si	P	S	Cl	Ar	
4	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	
	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
5	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	
	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
6	55	56	57	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	
	Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
7	87	88	89	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	
	Fr	Ra	Ac	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og	
lanthanoid series	6	58	59	60	61	62	63	64	65	66	67	68	69	70	71				
		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu				
actinoid series	7	90	91	92	93	94	95	96	97	98	99	100	101	102	103				
		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr				

*Numbering system adopted by the International Union of Pure and Applied Chemistry (IUPAC). © Encyclopædia Britannica, Inc.

Physical properties

The Only insulator in Transition metal dichalcogenides(TMD)

- Charge density wave
- Superconductivity(not cover)
- Metal-insulator transition
- Quantum spin liquid

TaS₂ polytype

	2H	1T	1T'
Group & Structure	<ul style="list-style-type: none"> • P₆₃/mmc • Hexagonal (Trigonal prismatic) 	<ul style="list-style-type: none"> • P$\bar{3}m1$ • Hexagonal (Octahedral) 	<ul style="list-style-type: none"> • P₂₁/m • Monoclinic
Top View			
Side View			
Lattice Parameters	<ul style="list-style-type: none"> • a = b ≠ c • γ = 120 	<ul style="list-style-type: none"> • a = b ≠ c • γ = 120 	<ul style="list-style-type: none"> • α ≠ 90°

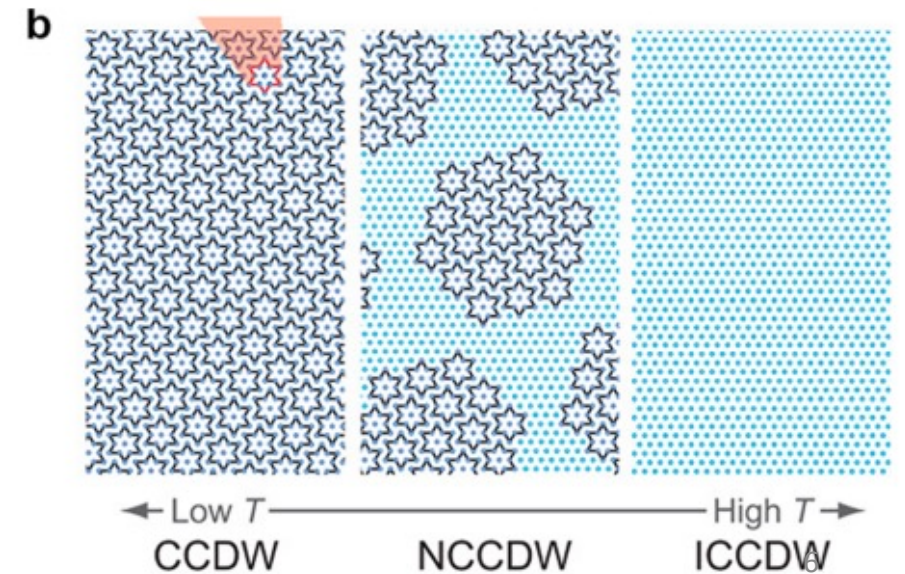
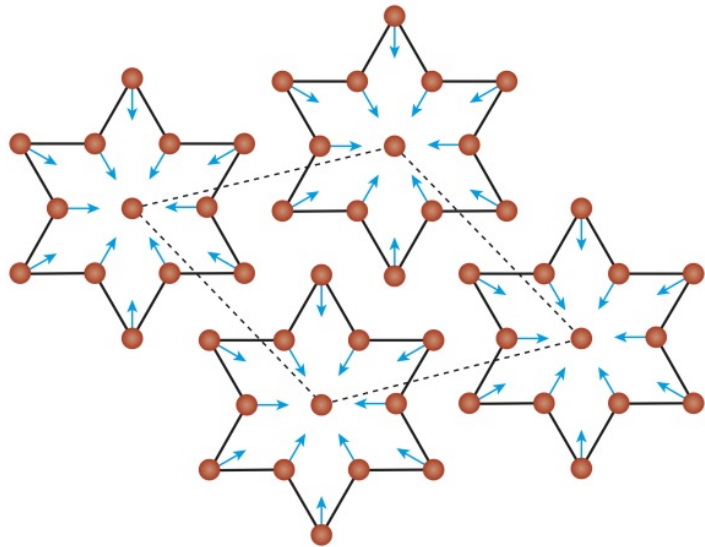
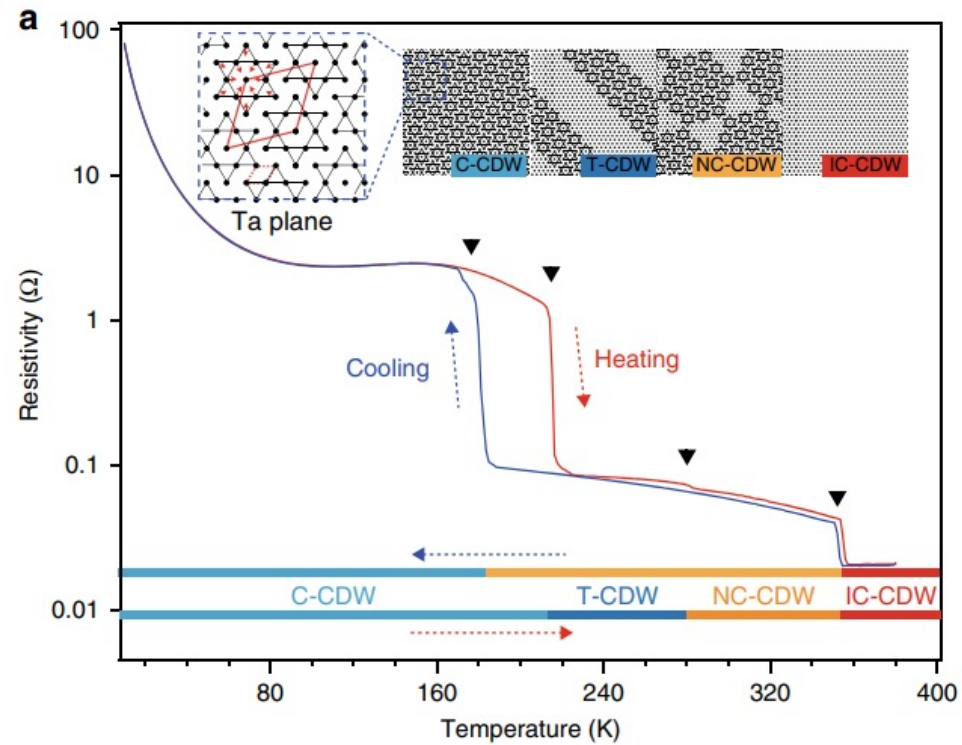
	T _d	3R	4H
Group & Structure	<ul style="list-style-type: none"> • Pmn2₁ • Orthorhombic 	<ul style="list-style-type: none"> • R3m • Rhombohedral 	<ul style="list-style-type: none"> • P6₃/mmc • Trigonal prismatic
Top View			
Side View			
Lattice Parameters	<ul style="list-style-type: none"> • a ≠ b ≠ c • β = 90 	<ul style="list-style-type: none"> • a = b ≠ c • γ = 120 	<ul style="list-style-type: none"> • a = b ≠ c • γ = 120

Physical properties

- Charge density wave
- Superconductivity(not cover)
- Metal-insulator transition
- Quantum spin liquid

1T-Charge density Wave(CDW)

- Commensurate
 - $\sqrt{13} \times \sqrt{13}$ supercell
 - Star of David (DoD)
- Nearly commensurate (below 350K)
- Incommensurate(below 180K)



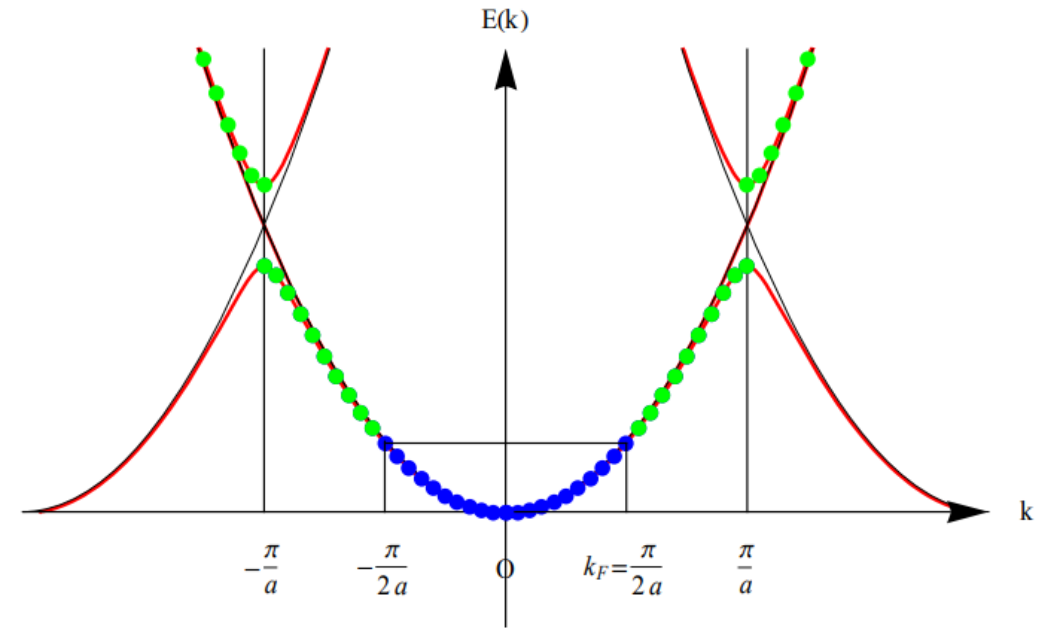
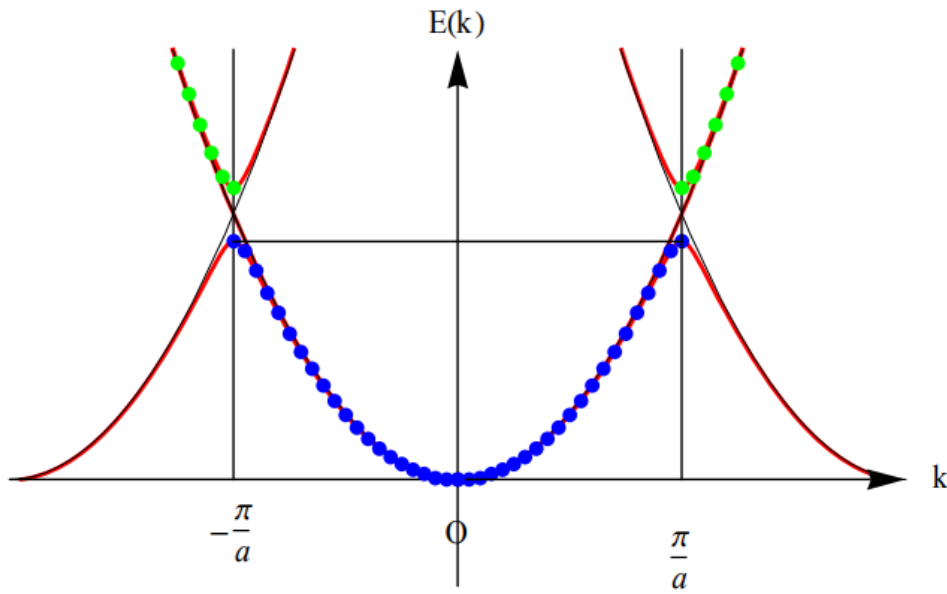
Charge density Wave (CDW)- Peierls picture



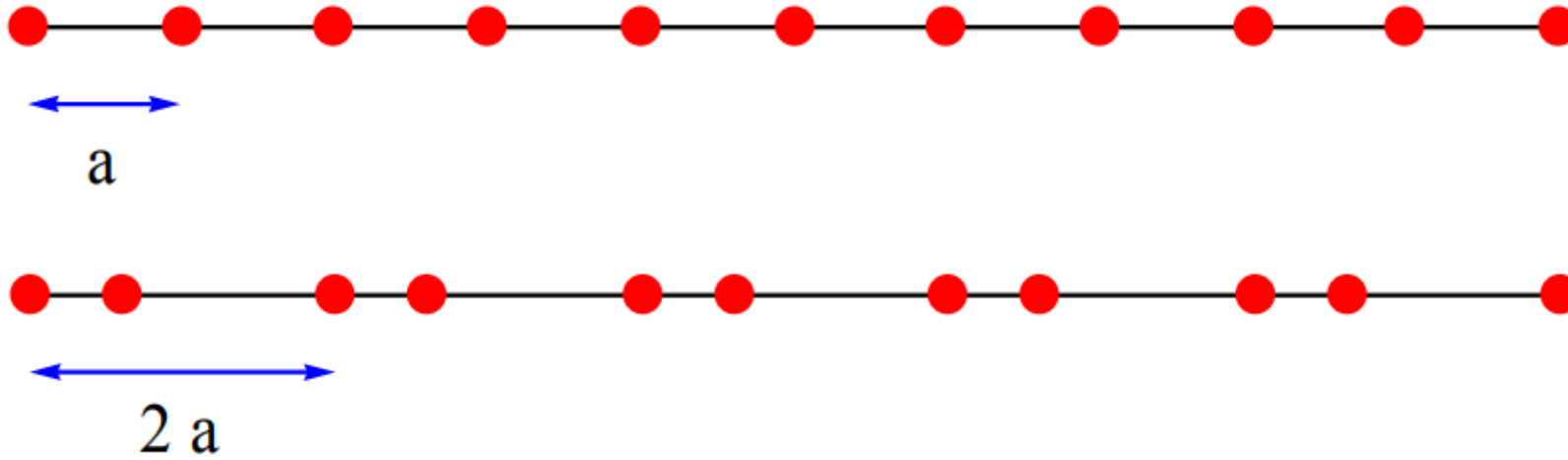
a

Insulator

Metal

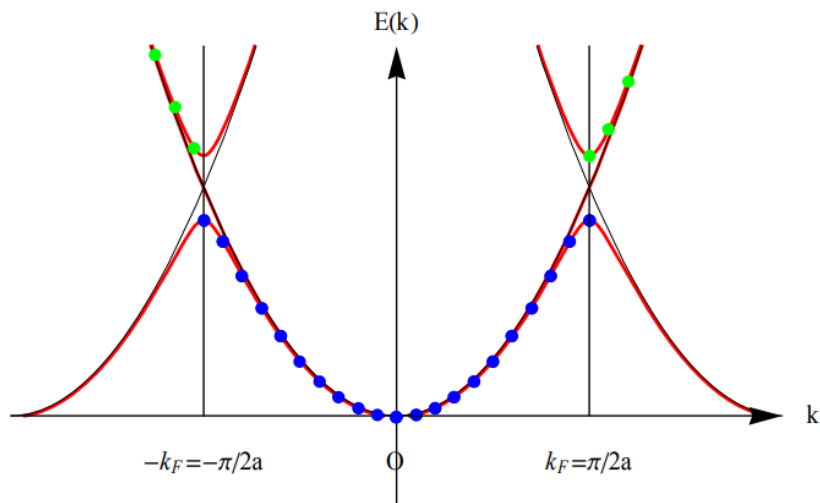


1D Peierls distortion



The system changes from metal to insulator (Peierls instability)

$$\Delta E = \Delta E_{\text{electronic}} + \Delta E_{\text{lattice}}$$



CDW Peierls distortion (continue)

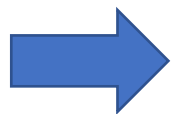
In 1D case, Peierls states that the system is always unstable, metal becomes insulator

Lindhard response- the response due to external perturbation

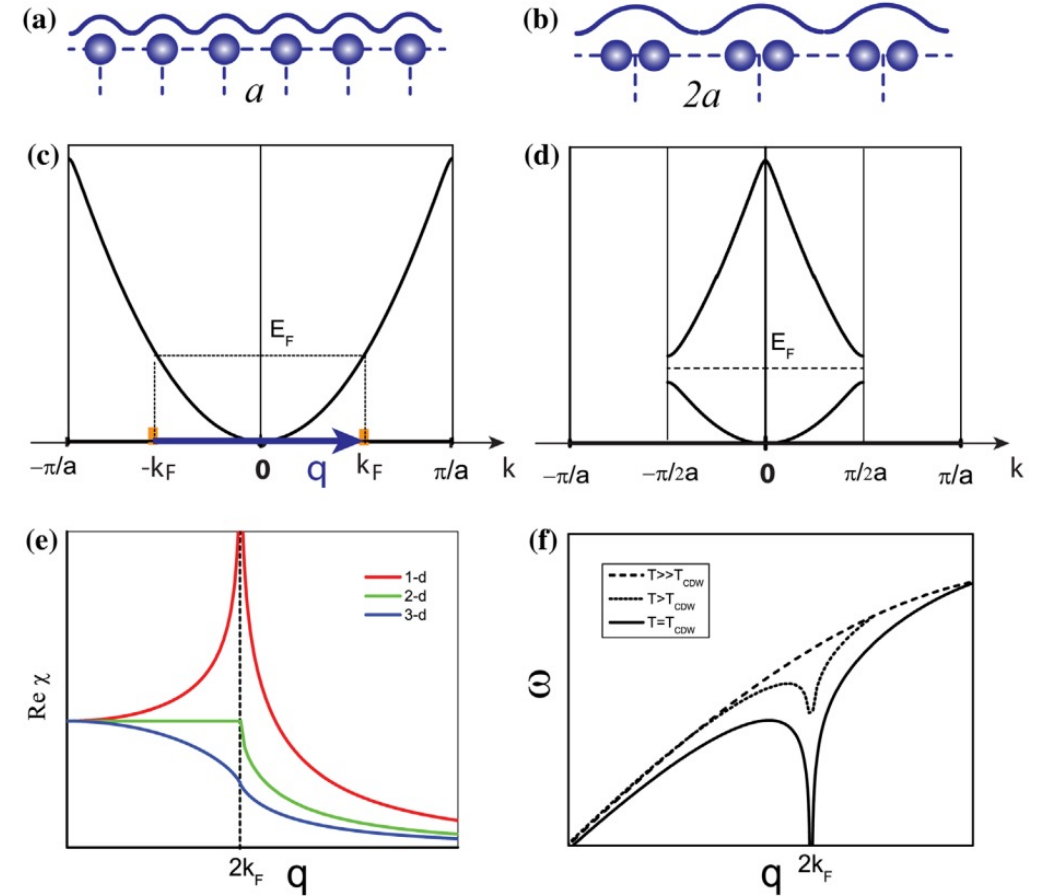
Frohlich Hamiltonian

$$\mathcal{H} = \sum_{\vec{k}} \varepsilon(\vec{k}) a_{\vec{k}}^+ a_{\vec{k}} + \sum_{\vec{q}} \hbar\omega(\vec{q}) b_{\vec{q}}^+ b_{\vec{q}} + \sum_{\vec{k}, \vec{q}} g(\vec{q}) a_{\vec{k}+\vec{q}}^+ a_{\vec{k}} (b_{-\vec{q}}^+ + b_{\vec{q}}),$$

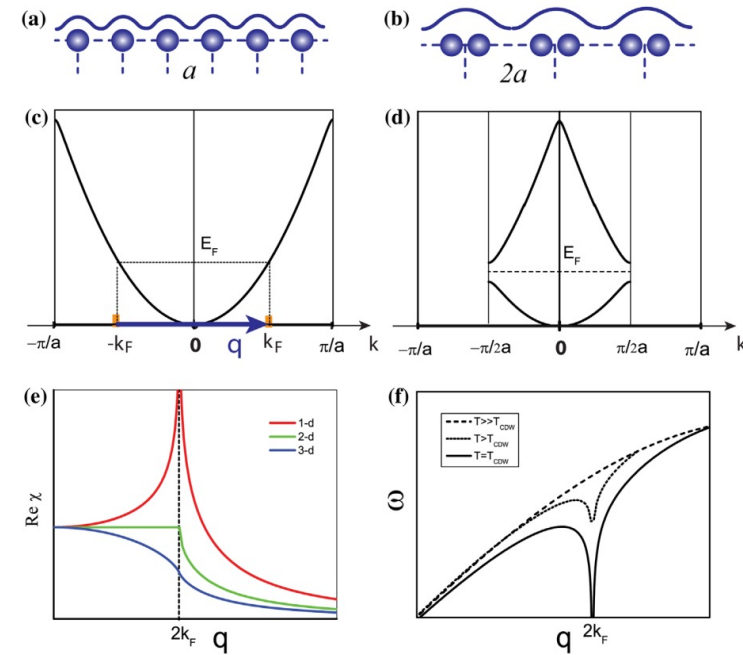
$$\tilde{\omega}(\vec{q})^2 = \omega(\vec{q})^2 + 2\omega(\vec{q}) |g(\vec{q})|^2 \text{Re}[\chi(\vec{q}, \omega)],$$



Kohn anomaly



Type 1	Quasi 1D Peierls picture
Type 2	Electron-phonon coupling but no fermi surface nesting
Type 3	No electron-phonon coupling no fermi surface nesting



	Peierls' model (1D atomic chain)	TTF-TCNQ (Quasi-1D material)	NbSe ₂ (Qua- si-2D material)	Sn/Ge or Pb/ Ge (2D films on surface)	Cuprates
Fermi Surface Nesting	√	√ [27]	X [30–32]	√ [37,38]	√ [64,69,70]
Sharp Peak in Lindhard Function	√	√ [23]	X [30–32]	√ [38]	√ [32]
Kohn Anomaly	√	√ [25]	√ [20]	√ [39,40]	X [32]
Structural Tran- sition	√	√ [24]	√ [15–19]	√ [37,38]	√ [67,68]
Metal–insulator Transition	√	√ [22]	X [34]	√ [37]	X [69]

Really Brief on Density Functional Theory

$$H_{\text{tot}} = \sum_j \frac{\mathbf{P}_j^2}{2M_j} + \sum_i \frac{\mathbf{p}_i^2}{2m} + \sum_{i < i'} \frac{Z_j Z_{j'} e^2}{|\mathbf{R}_j - \mathbf{R}_{j'}|} + \sum_{i < i'} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_{i'}|} + \sum_{ij} \frac{-Z_j e^2}{|\mathbf{R}_j - \mathbf{r}_i|}.$$

$$H = \sum_i \frac{\mathbf{p}_i^2}{2m} + \sum_i v(\mathbf{r}_i) + \frac{1}{2} \sum_{i \neq j} \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|}$$

$$\longrightarrow E_v[\rho] = \int v(\mathbf{r})\rho(\mathbf{r})d\mathbf{r} + T_s[\rho] + \frac{1}{2}e^2 \int \frac{\rho(\mathbf{r})\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}d\mathbf{r}' + E_{\text{xc}}[\rho]. \quad T_s[\rho] = -\frac{\hbar^2}{2m} \sum_i^{\text{occ}} \int \phi_i^*(\mathbf{r})\nabla^2\phi_i(\mathbf{r}) d\mathbf{r}$$

$$\left\{ \frac{p^2}{2m} + v(\mathbf{r}) + v_{\text{H}}(\mathbf{r}) + v_{\text{xc}}(\mathbf{r}) \right\} \phi_i(\mathbf{r}) = \epsilon_i \phi_i(\mathbf{r})$$

$$\rho(\mathbf{r}) = \sum_i^{\text{occ}} |\phi_i(\mathbf{r})|^2,$$

$$v_{\text{H}}(\mathbf{r}) = e^2 \int \frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}',$$

$$v_{\text{xc}}(\mathbf{r}) = \frac{\delta E_{\text{xc}}}{\delta \rho(\mathbf{r})}.$$

Functional benchmark

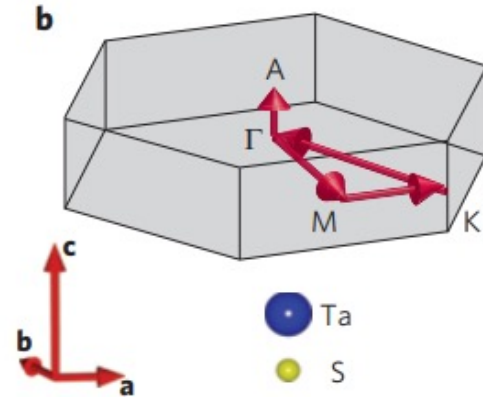
	<i>1T</i>	<i>2H-AB</i>	<i>2H-AA'</i>	<i>3R</i>
EXX+RPA				
a (Å)	3.362	3.316	3.310	3.310
c (Å)	5.90	12.25	12.05	18.30
ΔE (eV/f.u.)	0.084	0.010	0.00	0.010
optB86b-vdW				
a (Å)	3.352	3.317	3.320	3.317
c (Å)	5.90	12.30	12.00	18.30
ΔE (eV/f.u.)	0.063	0.016	0.00	0.008
Experiment				
a (Å)	3.3672(6) ^a	3.314 ^b		3.32 ^c
c (Å)	5.9020(9) ^a	12.097 ^b		17.90 ^c

Petr Lazar, Jana Martinová, and Michal Otyepka Phys. Rev. B **92**, 224104 – Published 8 December 2015

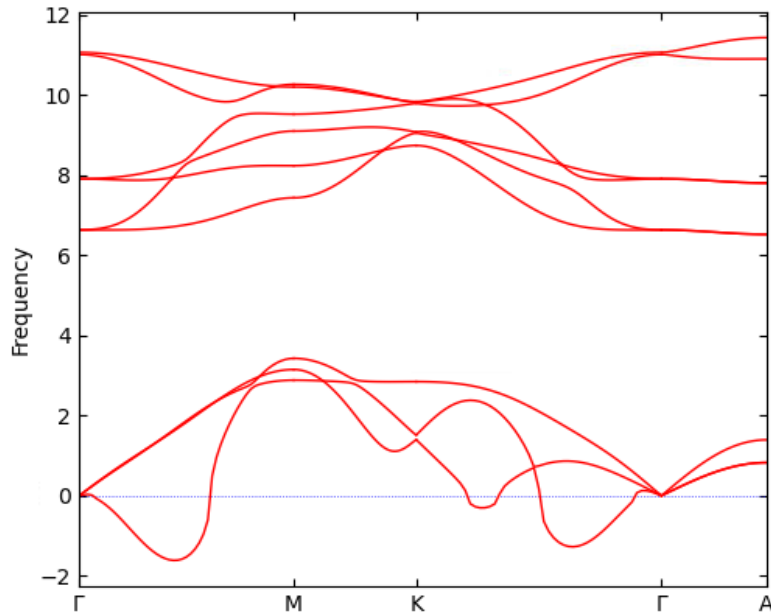
1T	a	c
pbe	3.377	6.947
opt86b	3.3484	5.932
Scan	3.365	6.118
rVV10 - 6.3	3.416	6.079
rVV10 - 15.7	3.416	6.079

2H	a	c
pbe	3.341	13.758
opt86b	3.317	12.0653
pbe-vdW	3.35	12.461
DF2-B86R	3.319	12.05
scan	3.325	12.751
Scan-af	3.326	12.786
rVV10 -6.3	3.369	12.467
rVV10-15.7	3.369	12.467

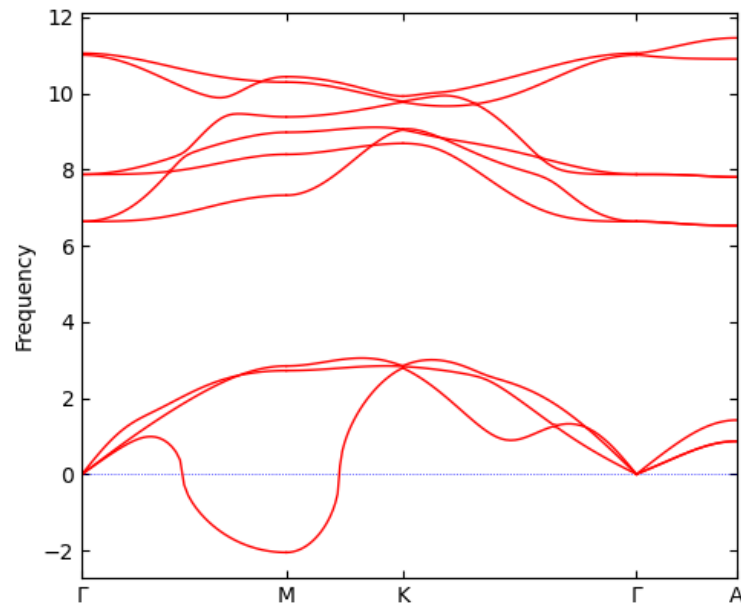
1T phonon



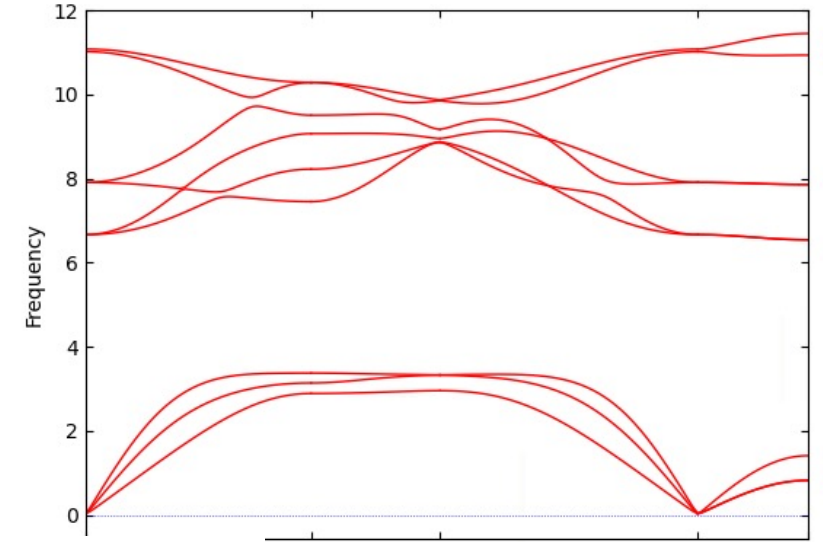
“4 4 2” finite diff
Gaussian smearing 0.1



“3 3 2” finite diff
Gaussian smearing 0.1



“2 2 2” density functional perurbation theory
MP smearing 0.1

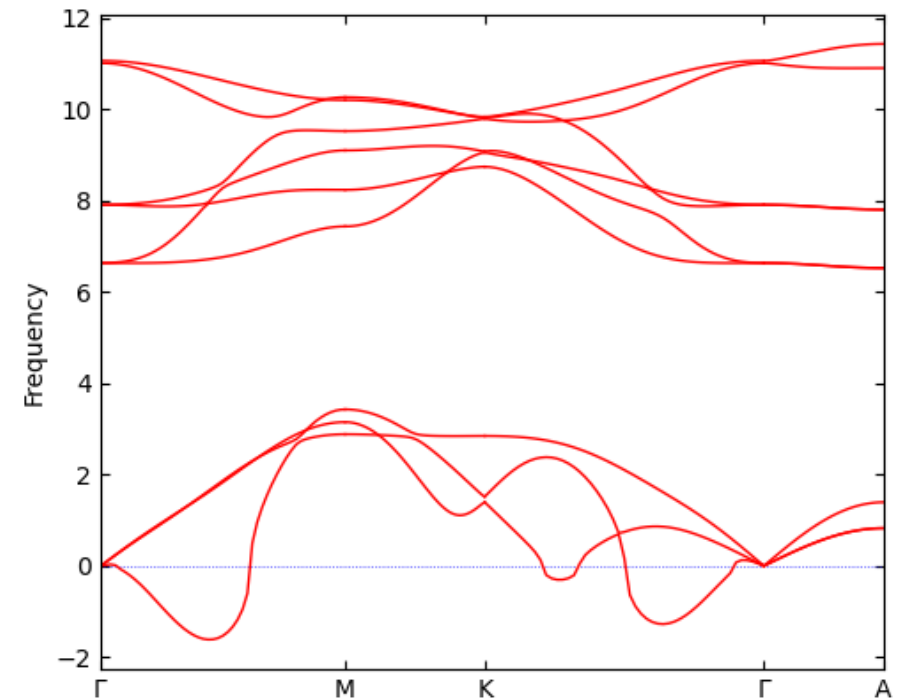
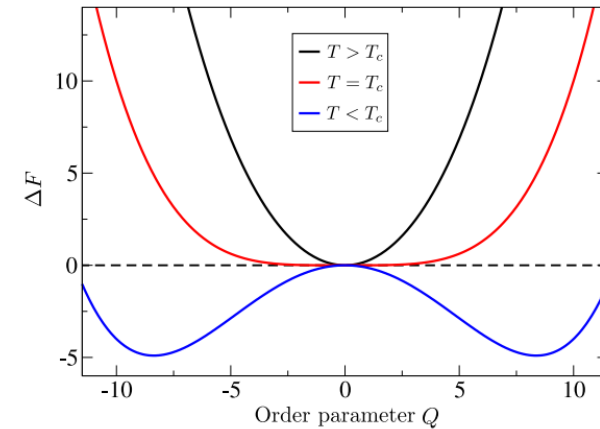


1T CDW is has 13 unitcells in plane

Imaginary phonon mode

- Calculation might be done wrong
 - Phonon calculation needs extremely precise calculation (VASP EDIFF = 1 E-8)
 - Sensitive to supercell you construct
 - Cut-off energy k point density
- Some interesting physics happens
 - Negative curvature for Potential energy surface
 - Higher order Anharmonic effects need to be considered
 - Phonon-phonon coupling
 - System is dynamically unstable
 - Ferroelectric (PbTiO₃)
 - Superionic conduction (Li₃N)
 - CDW

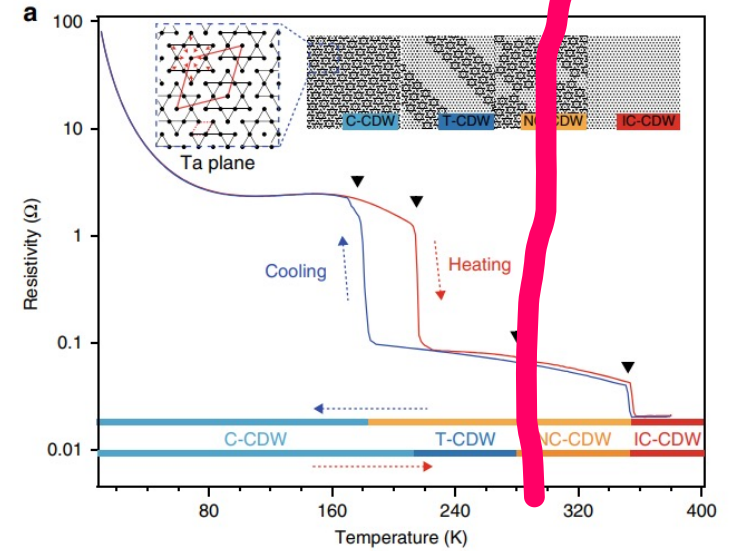
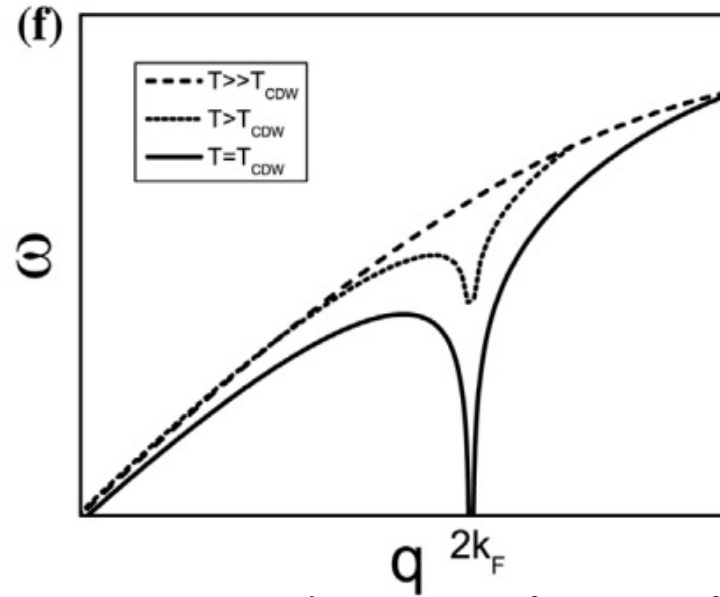
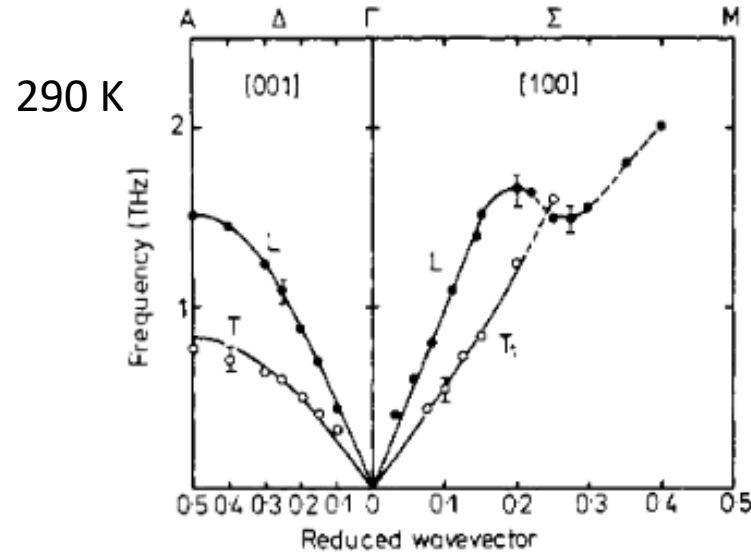
The Physical Significance of Imaginary Phonon Modes in Crystals [Ioanna Pallikara](#), [Prakriti Kayastha](#), [Jonathan M. Skelton](#), [Lucy D. Whalley](#) [arXiv:2203.01244](#)



Phonon

- Harmonic approximation
 - Frozen Phonon (Supercell approach)
 - Density functional perturbation Theory(DFPT)
- To consider anharmonic effect and temperature dependence
 - stochastic self-consistent harmonic approximation(SSCHA)
 - Mapping from AIMD
 - Self-consistent phonon(SCPH)

Experiment data for Kohn anomaly



F. Clerc, C. Battaglia, M. Bovet, L. Despont, C. Monney, H. Cercellier, M. G. Garnier, P. Aebi, H. Berger, and L. Forró Phys. Rev. B 74, 155114 – Published 17 October 2006

TaS2
Quasi-2D

yes

?

yes

Yes and no

K R A Ziebeck et al 1977 J. Phys. F: Met. Phys. 7 1139

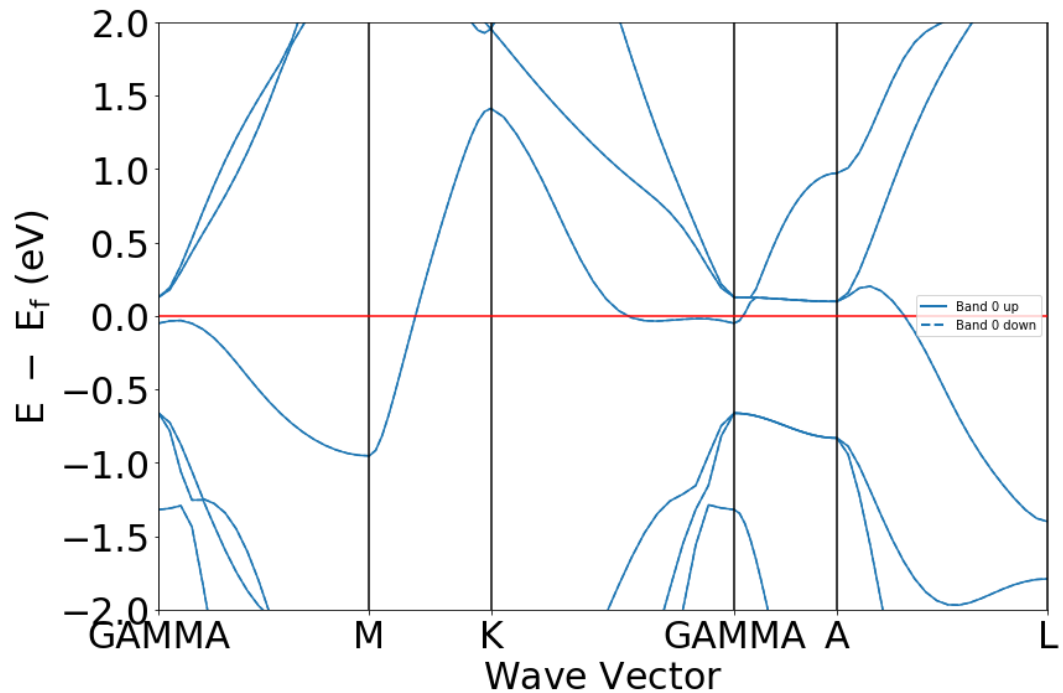
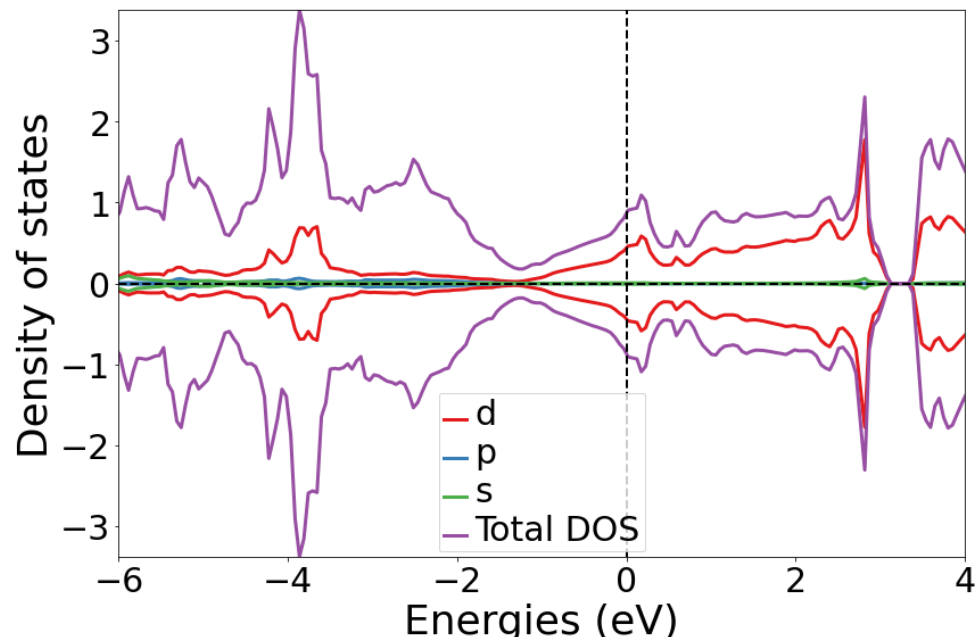
	Peierls' model (1D atomic chain)	TTF-TCNQ (Quasi-1D material)	NbSe ₂ (Quasi-2D material)	Sn/Ge or Pb/Ge (2D films on surface)	Cuprates
Fermi Surface Nesting	✓	✓ [27]	X [30–32]	✓ [37,38]	✓ [64,69,70]
Sharp Peak in Lindhard Function	✓	✓ [23]	X [30–32]	✓ [38]	✓ [32]
Kohn Anomaly	✓	✓ [25]	✓ [20]	✓ [39,40]	X [32]
Structural Transition	✓	✓ [24]	✓ [15–19]	✓ [37,38]	✓ [67,68]
Metal–insulator Transition	✓	✓ [22]	X [34]	✓ [37]	X [69]

Physical properties

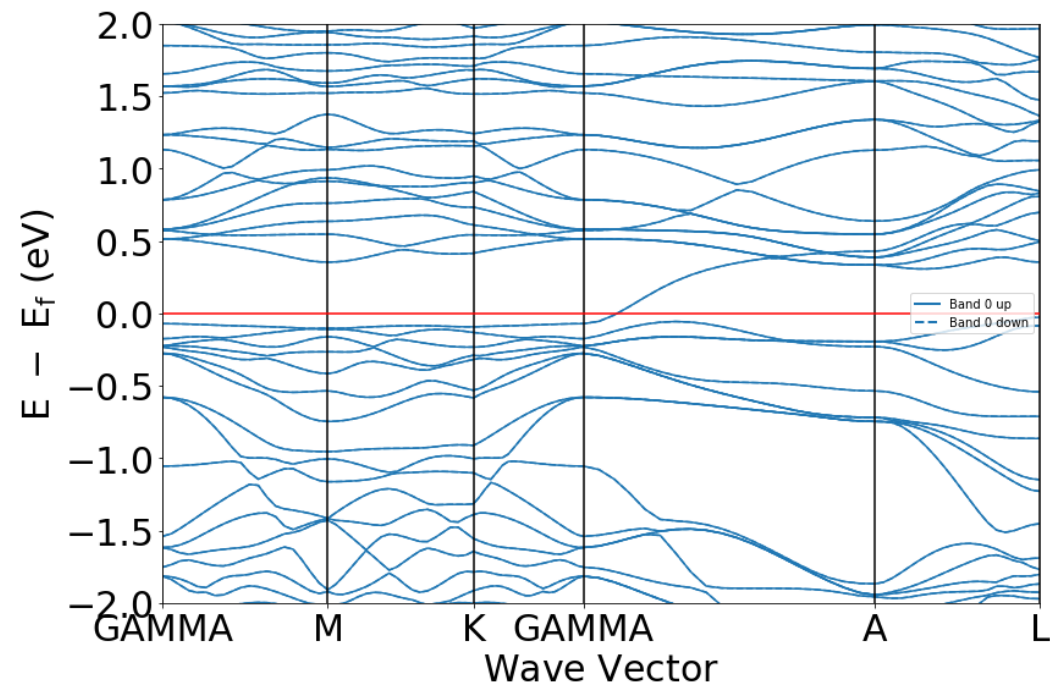
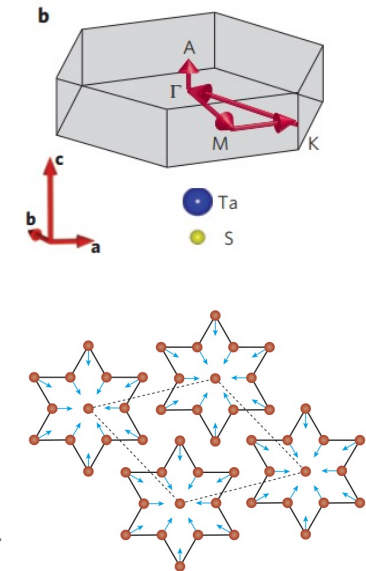
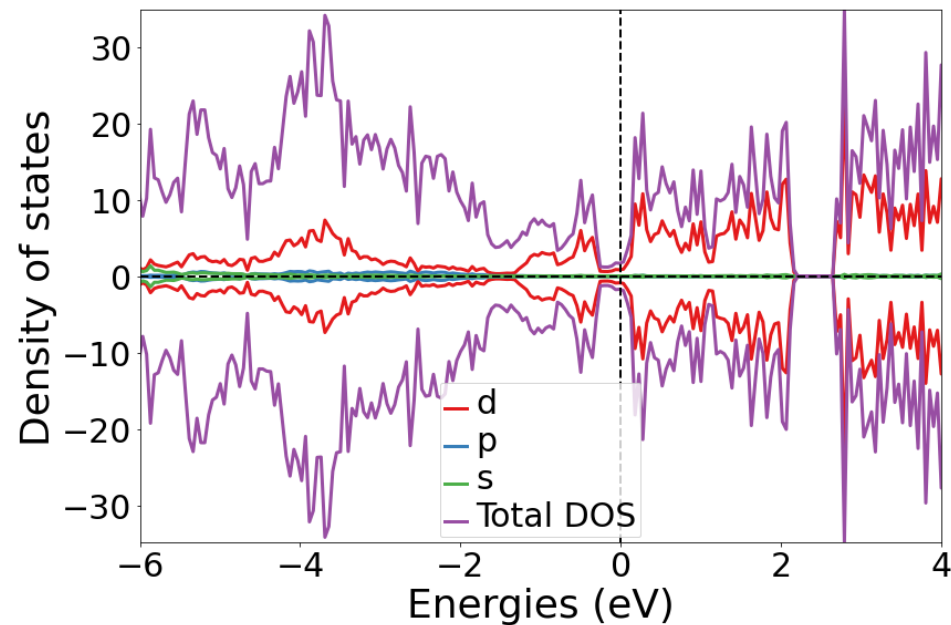
- Charge density wave
- Superconductivity(not cover)
- **Metal-insulator transition**
- Quantum spin liquid

TaS₂ considered to be mott insulator(maybe?)

undistorted



SOD

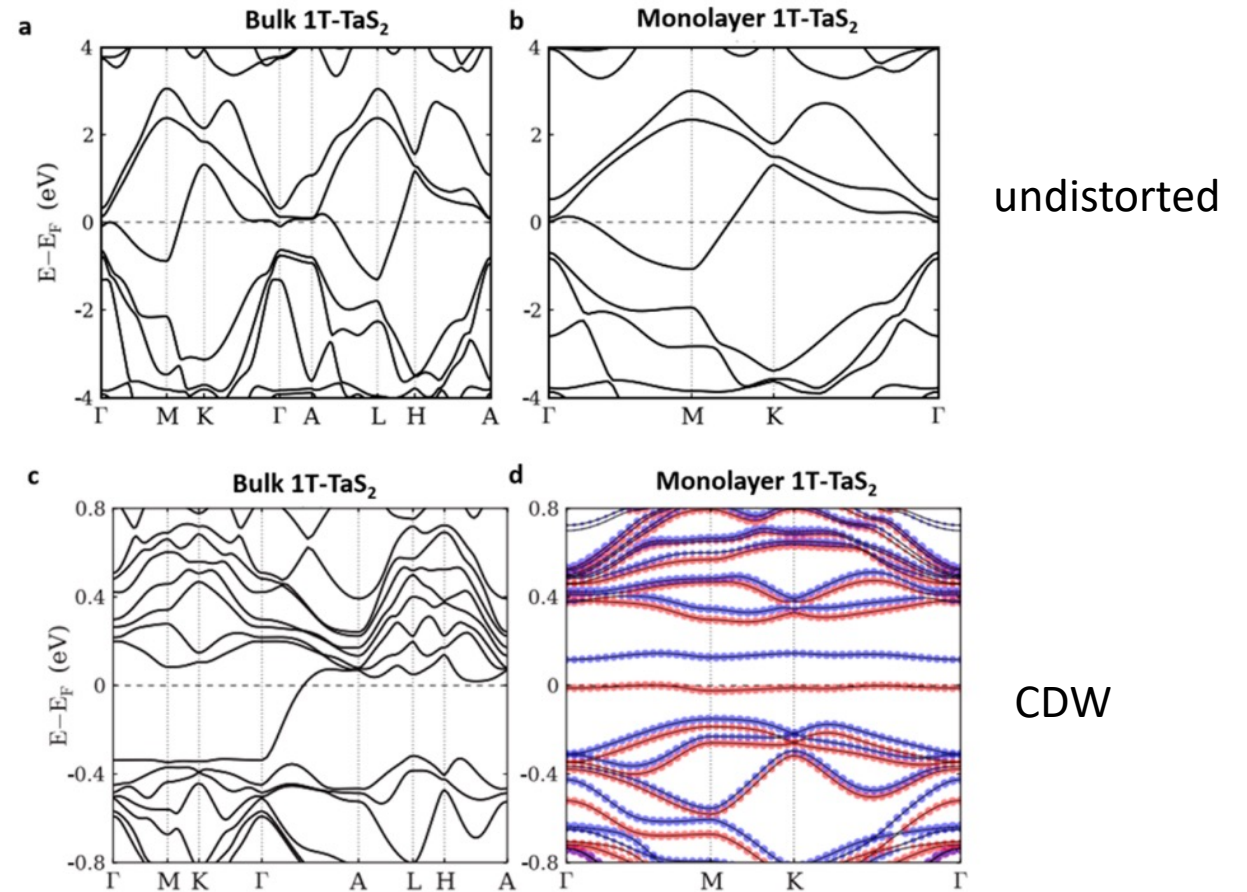
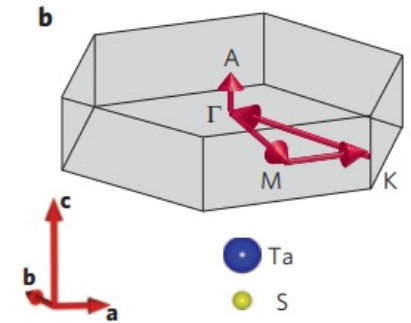
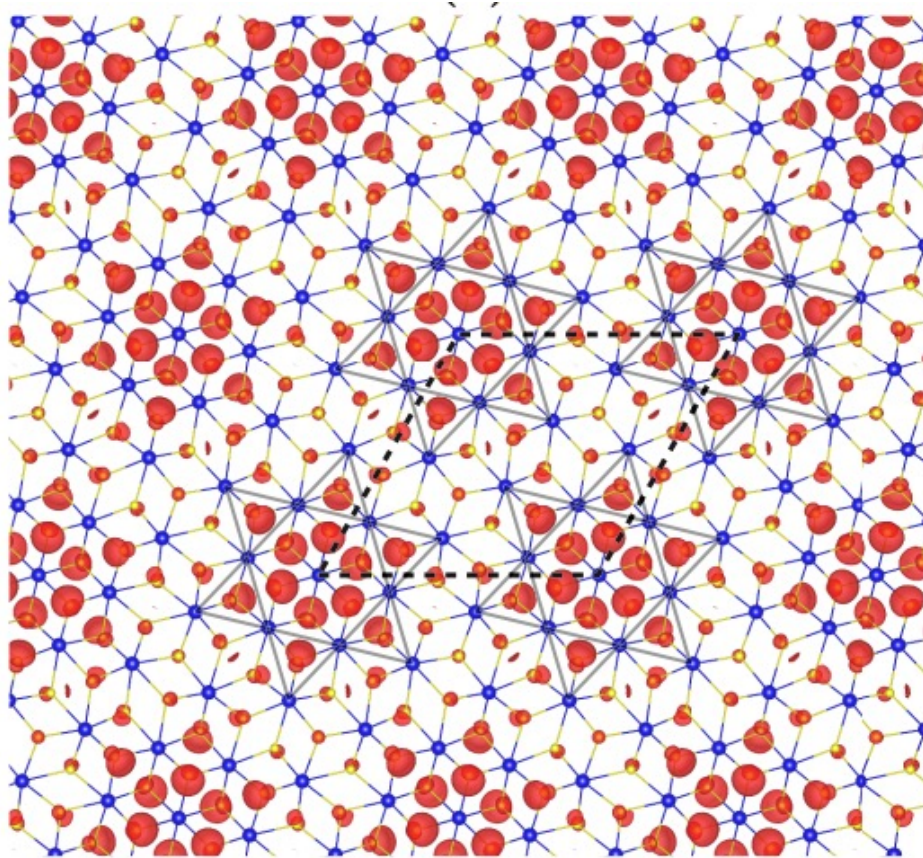


Computation report of gap opening

- Spin polarization in monolayer
- Using DFT+U in monolayer

Band gap by spin polarization

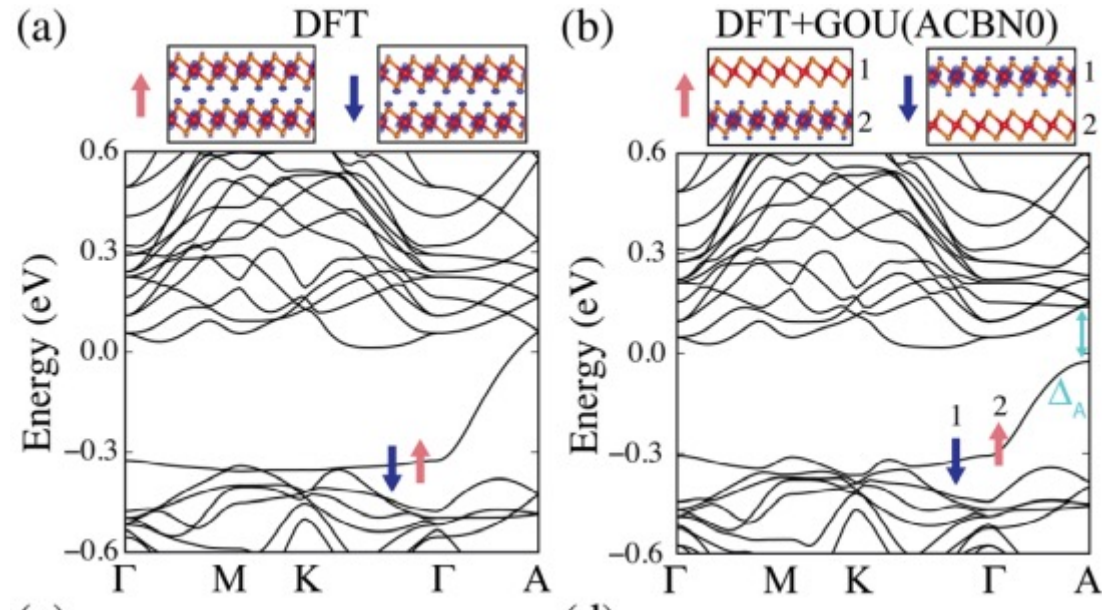
Charge density difference of undistorted and CDW



DFT+U

U is determined by self-consistent way (ACBN0)

CDW

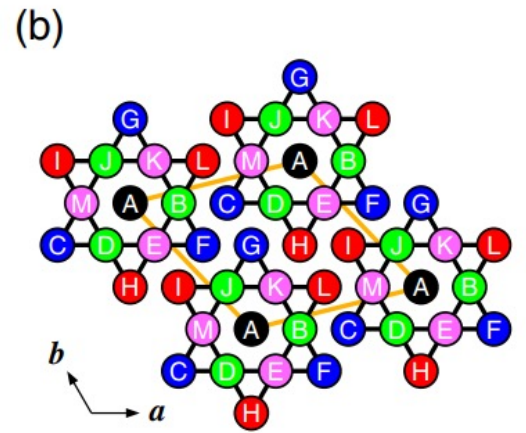


Conclusion:

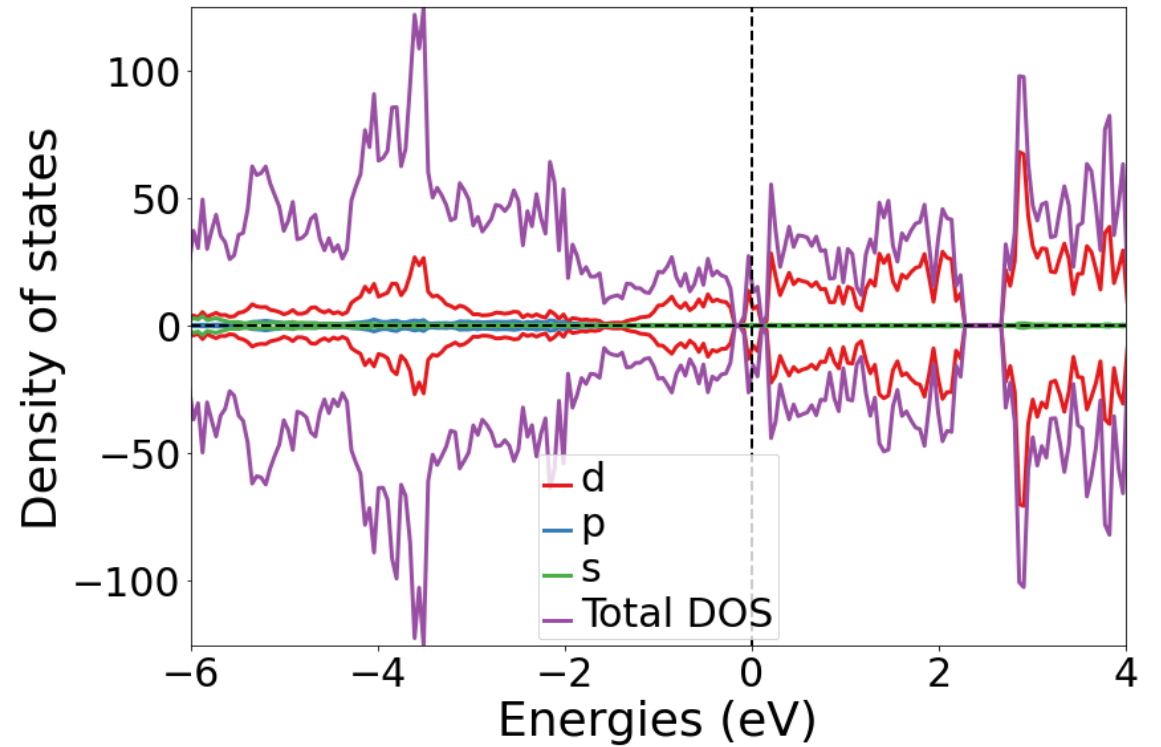
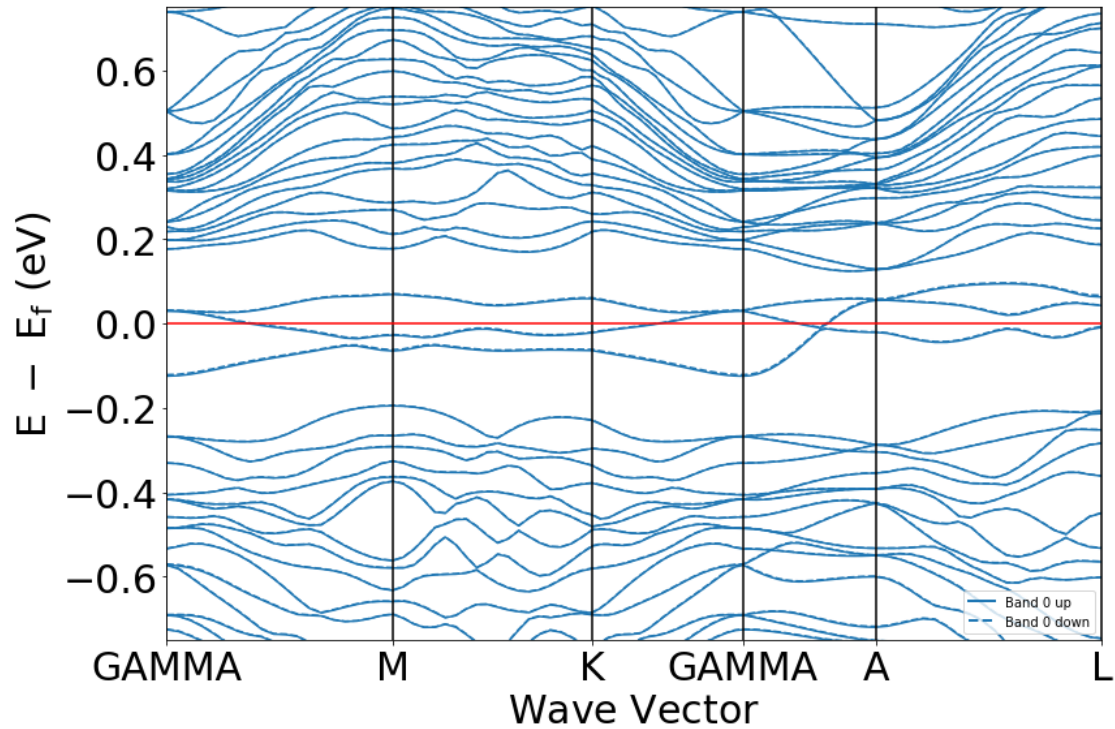
Spin polarization opens gap only for monolayer CDW not for bulk

DFT+U with self-consistent U indicates mott insulator

Some interesting band structure plot



AEB stacking

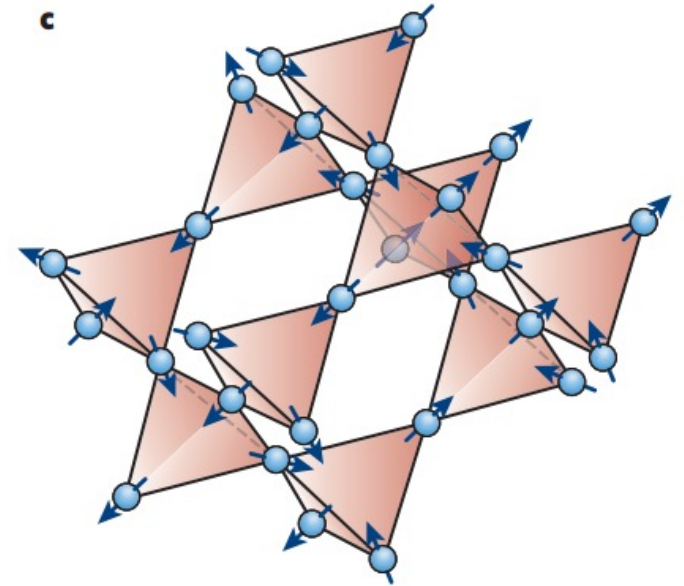
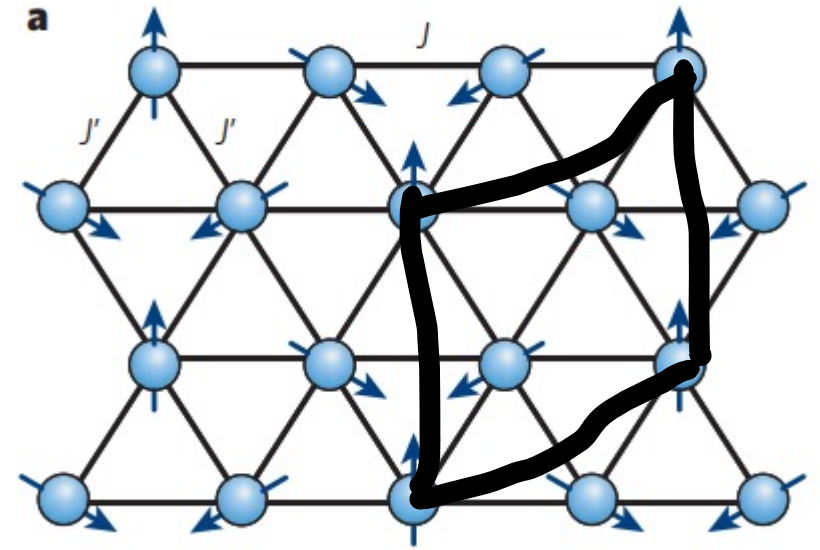
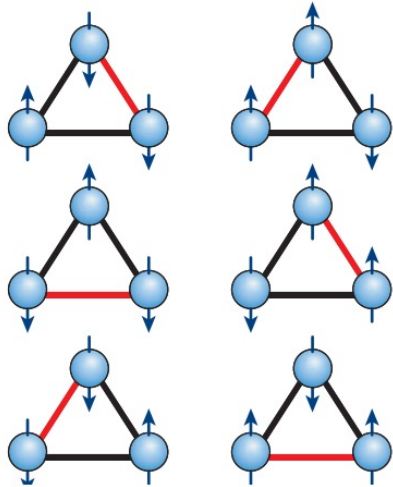


Physical properties

- Charge density wave
- Superconductivity(not cover)
- Metal-insulator transition
- **Quantum spin liquid**

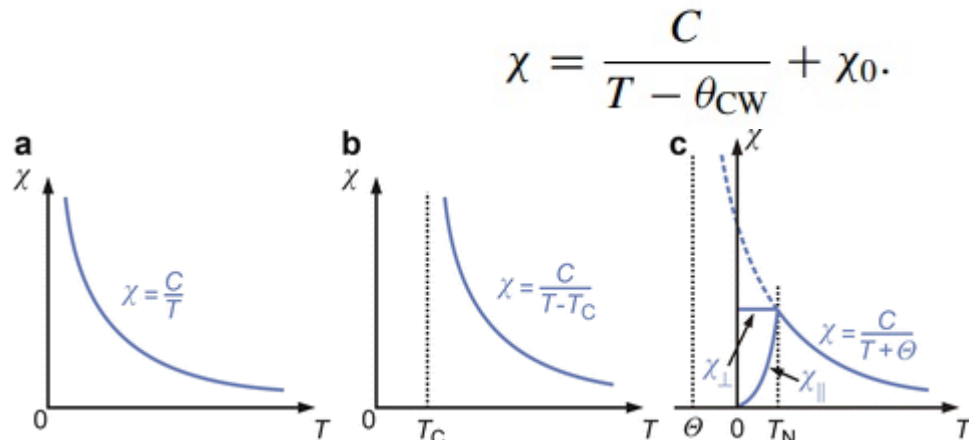
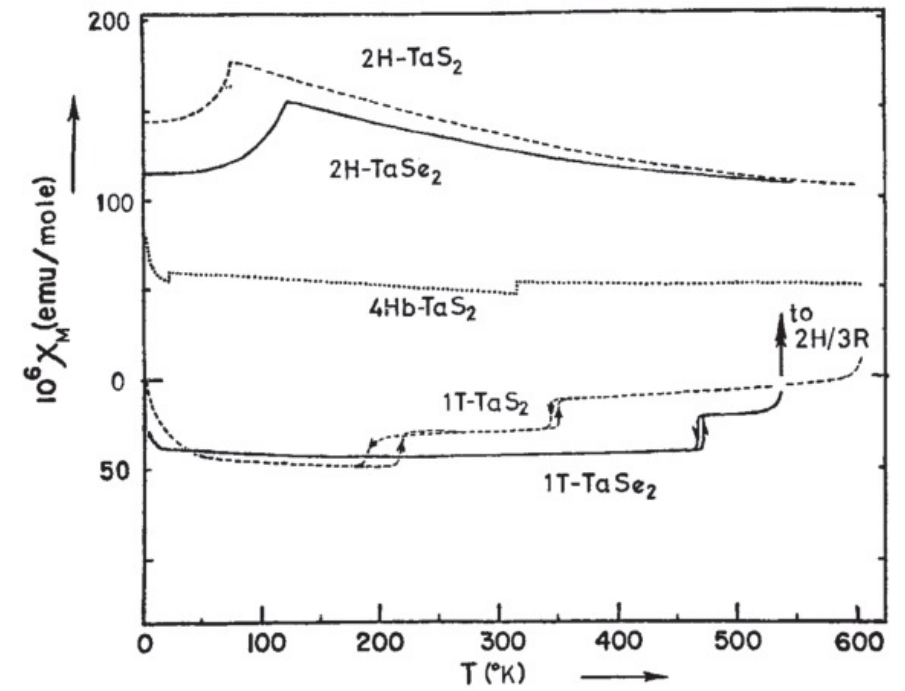
Quantum Spin Liquid(QSL)

- Non-magnetic, spin = 0
- Classical spin liquid: spin frozen at low T
 - Spin Ice- we somehow know the spin orientation
 - Triangular lattice antiferromagnet
- Quantum spin liquid:
 - Quantum fluctuation prevent magnetic order
 - Paramagnetic like ground state



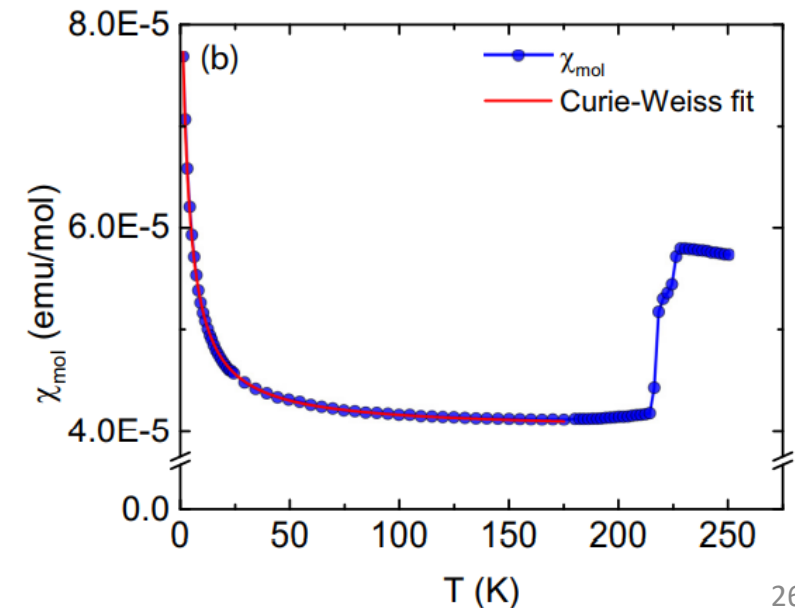
Quantum Spin Liquid(QSL)

- Lets say TaS2 in a mott insulator
 - The spins will form local moments, antiferromagnetic ground state
 - Or a QSL state which has paramagnetic behavior , following Curie Weiss Law



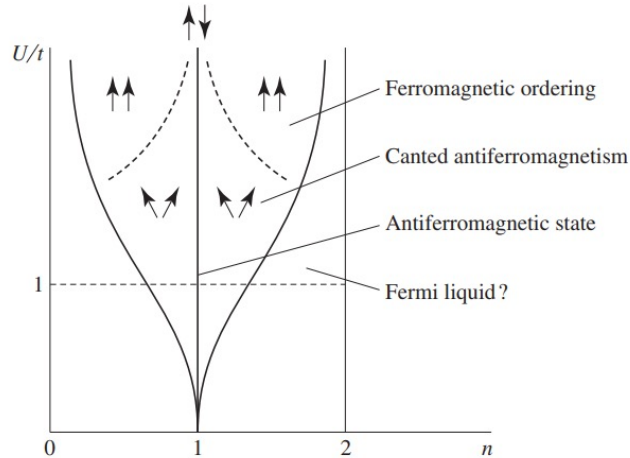
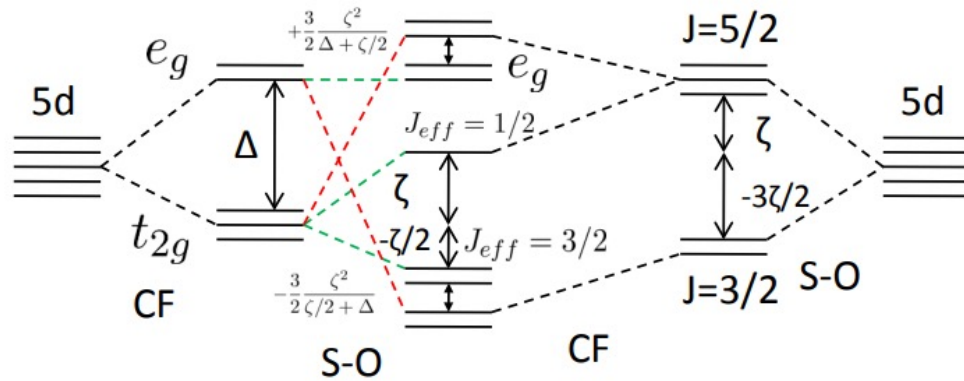
Law, K. T. & Lee, P. A. 1T-TaS₂ as a quantum spin liquid. *Proc. Natl. Acad. Sci. USA* **114**, 6996–7000 (2017).

Gapless excitations in the ground state of 1T-TaS₂ A. Ribak, I. Silber, C. Baines, K. Chashka, Z. Salman, Y. Dagan, and A. Kanigel *Phys. Rev. B* **96**, 195131 – Published 15 November 2017

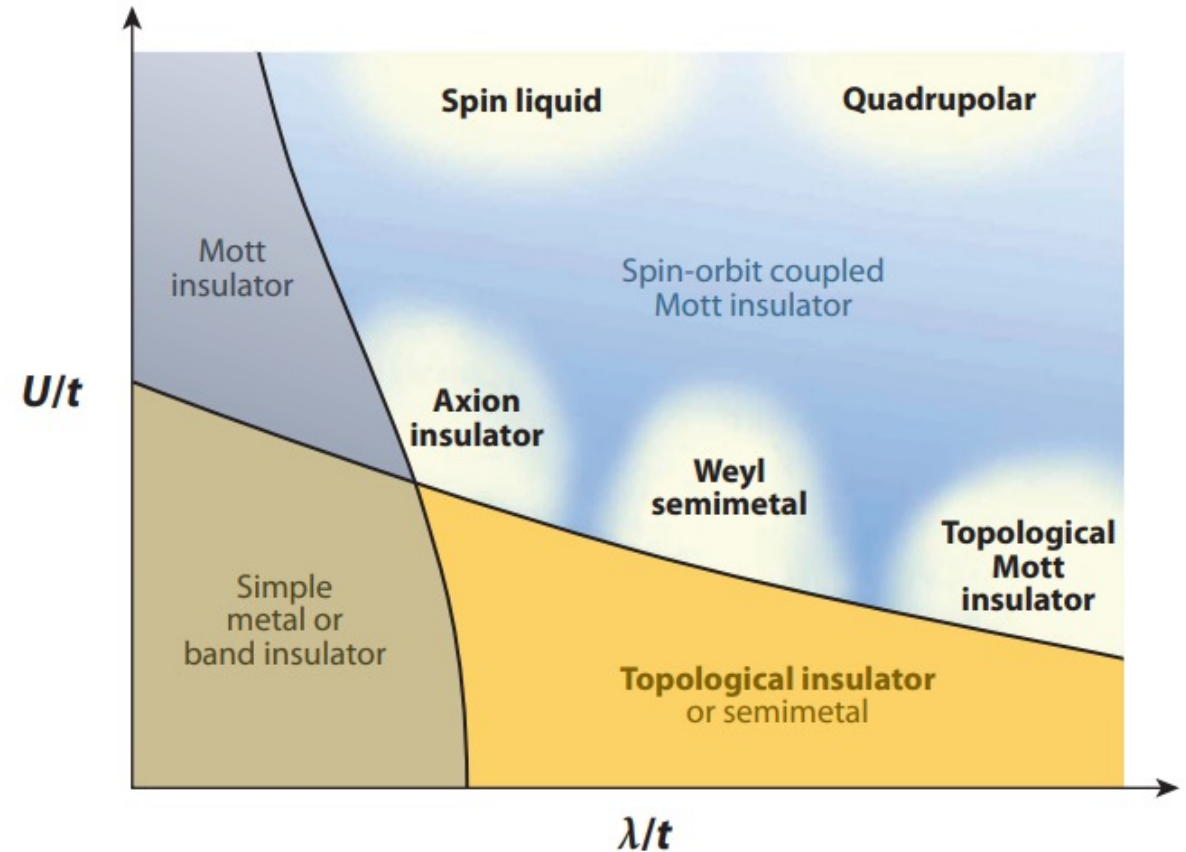


General discussion

Heavy element- spin orbit coupling



$$H = \sum_{i,j;\alpha\beta} t_{ij,\alpha\beta} c_{i\alpha}^\dagger c_{j\beta} + \text{h.c.} + \lambda \sum_i L_i \cdot S_i + U \sum_{i,\alpha} n_{i\alpha} (n_{i\alpha} - 1),$$



Khomsikii, D. (2014). *Transition Metal Compounds*. Cambridge: Cambridge University Press. doi:10.1017/CBO9781139096782

[Correlated Quantum Phenomena in the Strong Spin-Orbit Regime](#) William Witczak-Krempa, Gang Chen, Yong Baek Kim, Leon Balents Annual Review of Condensed Matter Physics 2014 5:1, 57-82

Mixing of t_{2g} - e_g orbitals in 4d and 5d transition metal oxides Georgios L. Stamokostas and Gregory A. Fiete Phys. Rev. B **97**, 085150 – Published 26 February 2018

General discussion continued

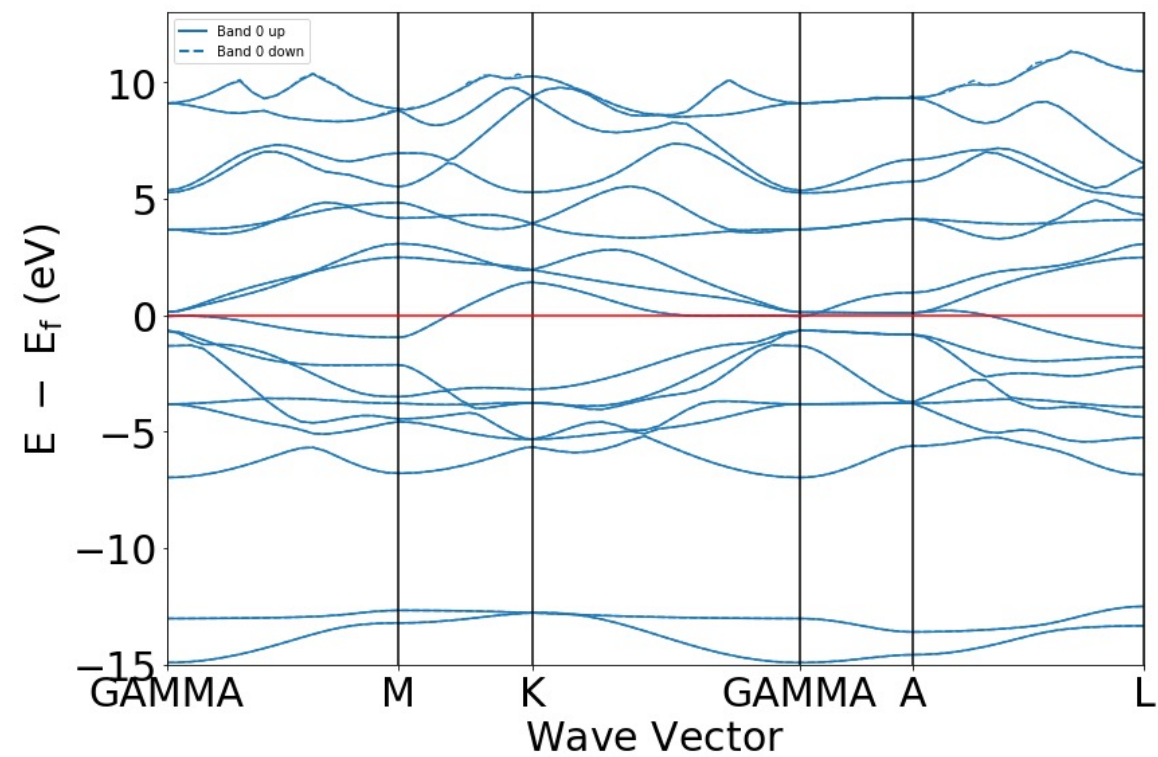
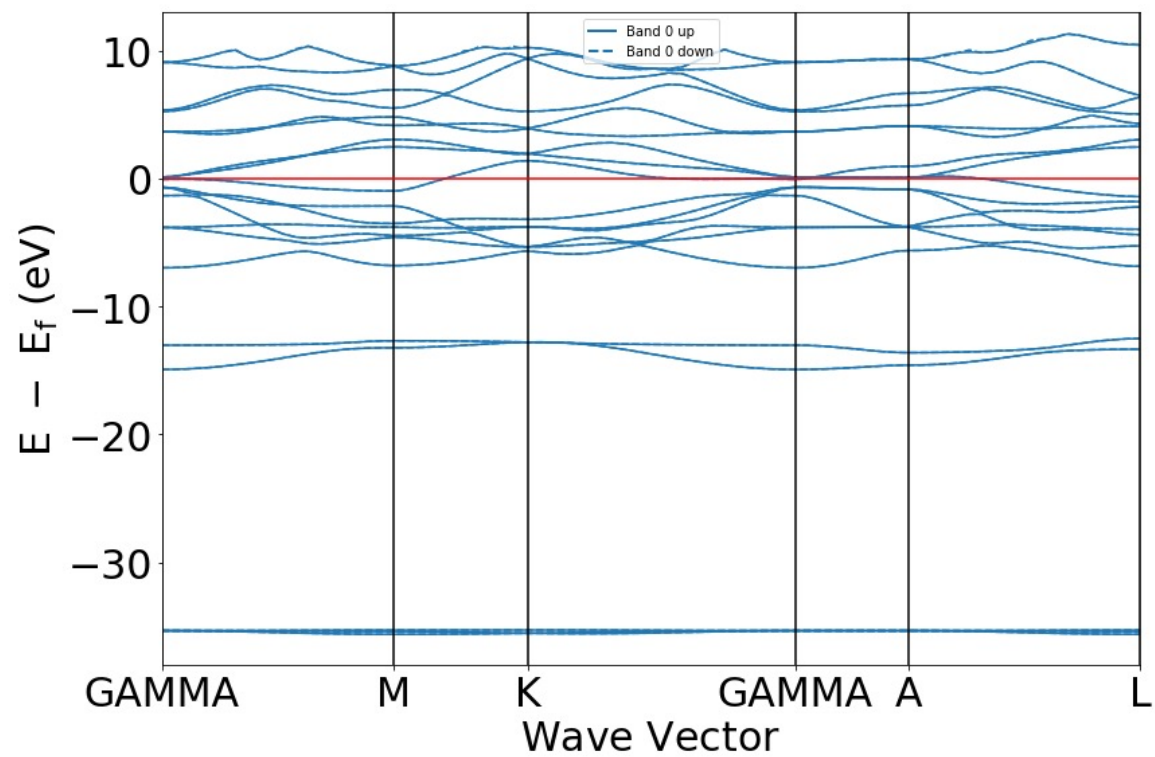
- Heavy element- spin orbit coupling
- Failure of VASP, scalar relativistic for valence electrons pseudopotential

$$E_n = -\frac{e^2}{8\pi\epsilon_0 a_0 n^2} \quad \mathcal{H}_{\text{Darwin}} = \frac{\hbar^2}{8m_e^2 c^2} 4\pi \left(\frac{Ze^2}{4\pi\epsilon_0} \right) \delta^3(\vec{r})$$

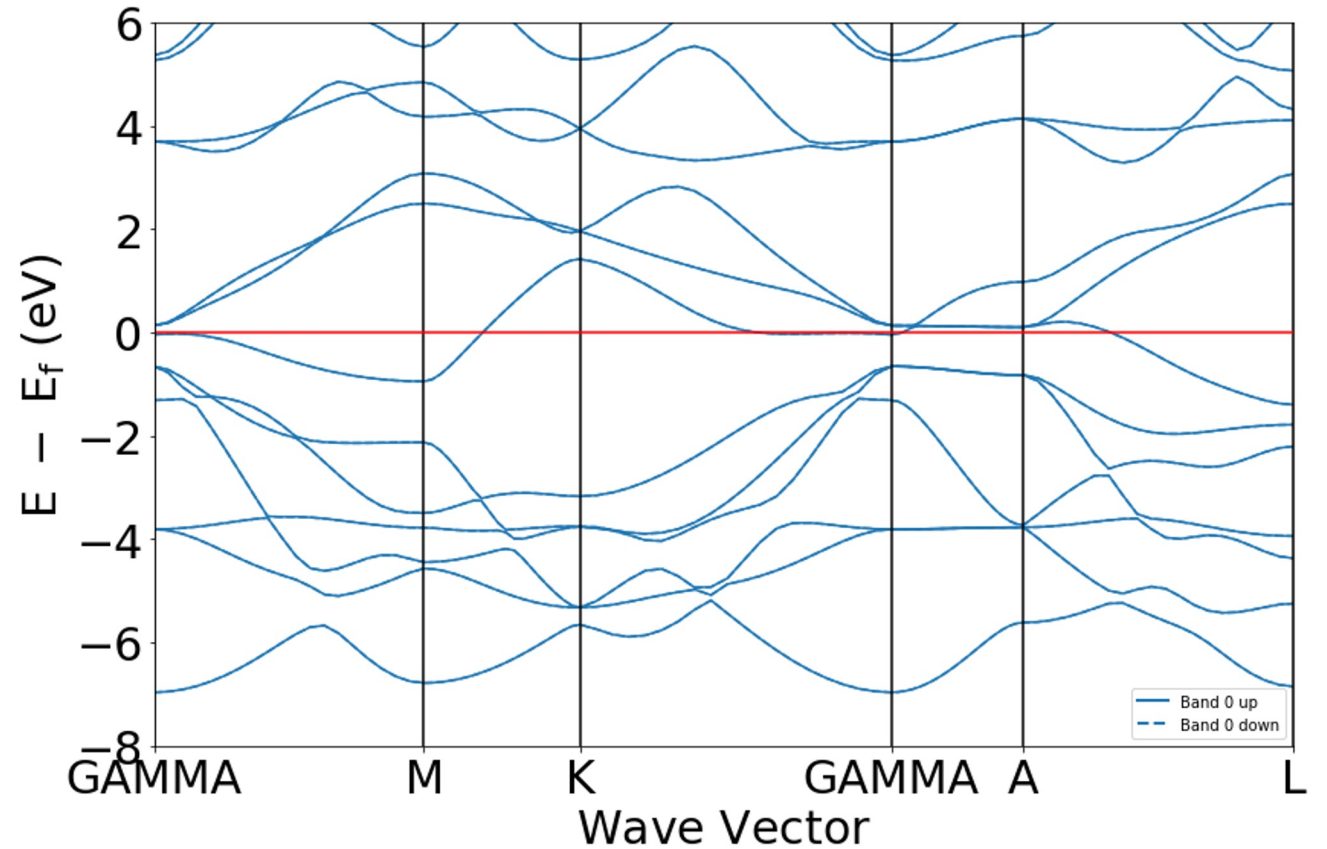
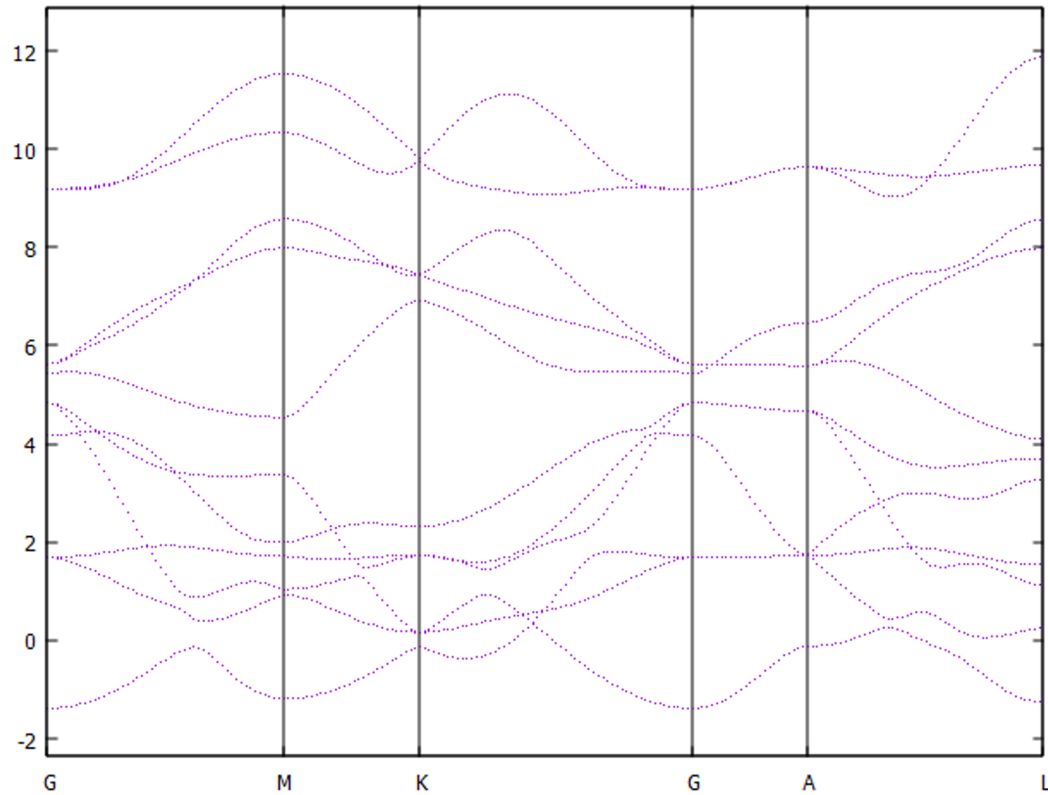
$$\mathcal{H}_{\text{SO}} = \left(\frac{Ze^2}{4\pi\epsilon_0} \right) \left(\frac{g_s - 1}{2m_e^2 c^2} \right) \frac{\vec{L} \cdot \vec{S}}{r^3}$$

- Failure of exchange-correlation, not treat it with many-body problem

- Questions



Wannier interpolation with 'Ta':d , 'S':p



Wannier orbital

