

# Oxide crystal structures and electron counts: The basics



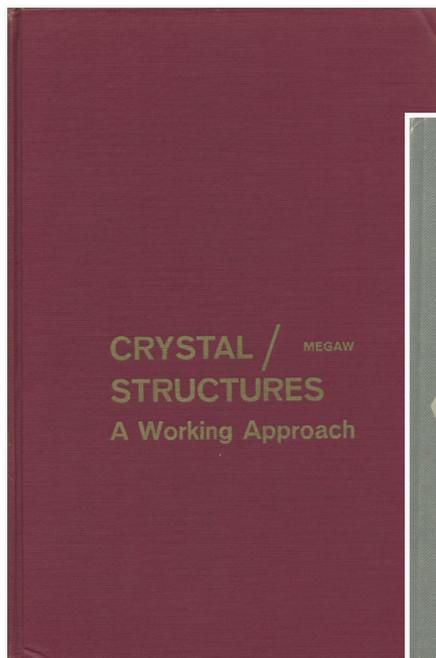
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seshadri@mrl.ucsb.edu

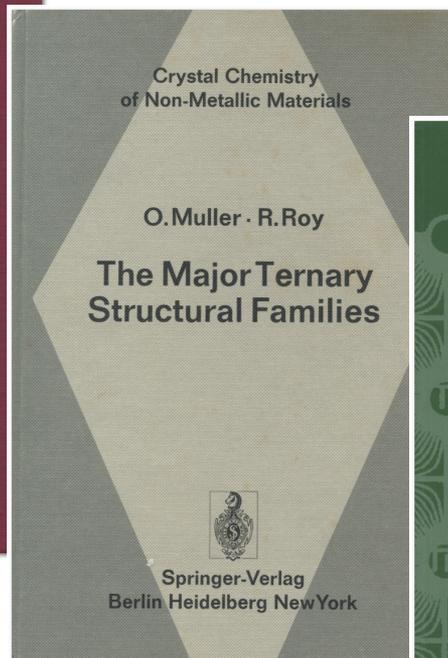
1. Brief description of oxide crystal structures (simple and complex)
  - a. Ionic radii and Pauling's rules
  - b. Electrostatic valence
  - c. Bond valence, and bond valence sums

*Why do certain combinations of atoms take on specific structures?*

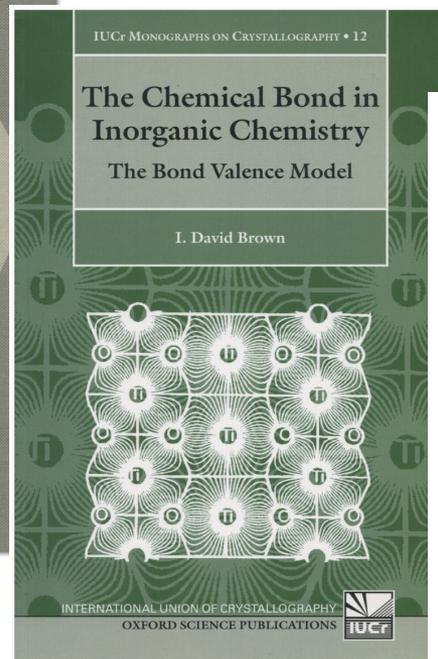
2. Counting electrons and simple electronic structures (largely avoiding transition metals)
3.  $d^0$  and  $s^2$  configurations.



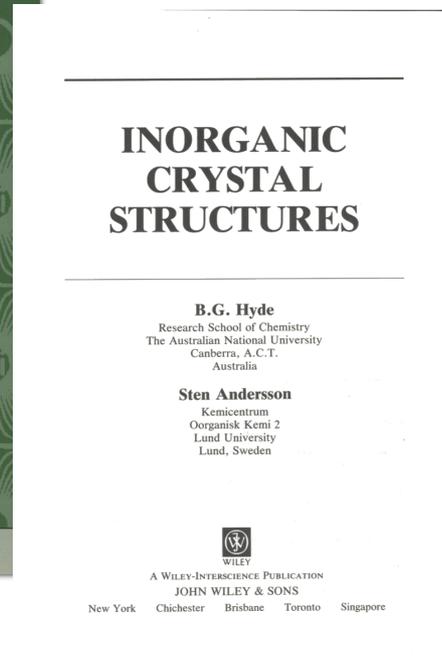
H. D. Megaw



O. Muller &  
R. Roy



I. D. Brown



B. G. Hyde &  
S. Andersson

CaMgSi2O6-pyroxene-diopside.vesta - VESTA

Step (°): 1.0 Step (px): 10 Step (θ): 10

CaMgSi2O6-pyroxene-diopside.vesta

**Tools** **Style** **Objects**

Structural models

Show models  
 Show dot surface

Style

Ball-and-stick  
 Space-filling  
 Polyhedral  
 Wireframe  
 Stick

Volumetric data

Show sections  
 Show isosurfaces  
 Surface coloring

Style

Smooth shading  
 Wireframe  
 Dot surface

Crystal shapes

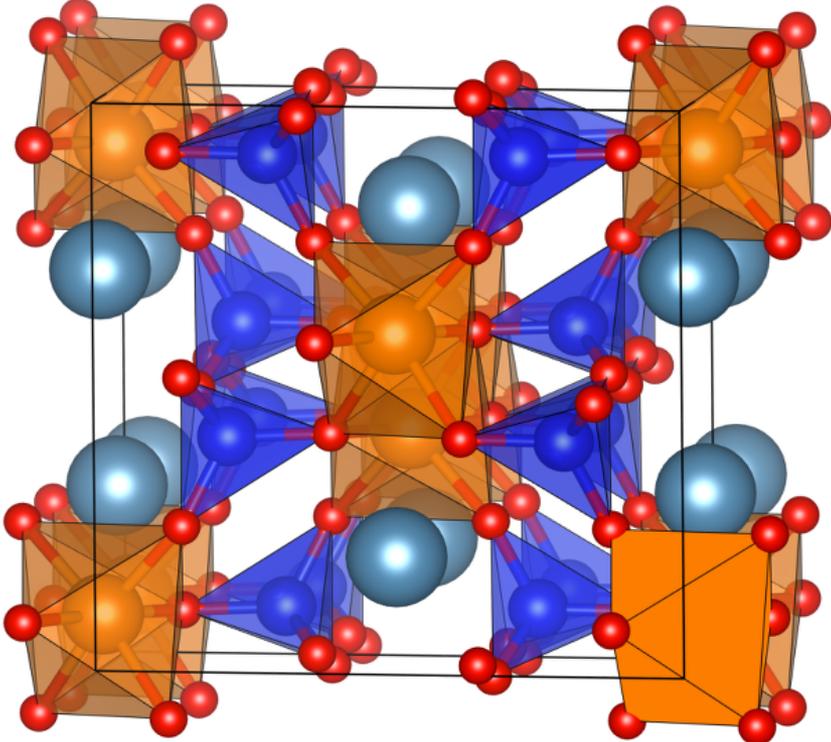
Show shapes

Style

Unicolor  
 Custom color  
 Wireframe

Properties...

Boundary... Orientation...



Q: Total charge received by the ion  
q: Formal charge (oxidation number)

		x	y	z	delta_q	Q	q
5	O3	0.88410	0.91230	-0.14230	0.353	-1.769	-2.000
4	O2	0.86150	0.74960	0.31960	0.356	-1.545	-2.000
5	O3	0.88410	1.08770	0.35770	0.291	-1.769	-2.000
4	O2	1.13850	0.74960	0.18040	0.356	-1.545	-2.000
5	O3	1.11590	0.91230	0.64230	0.353	-1.769	-2.000
5	O3	1.11590	1.08770	0.14230	0.291	-1.769	-2.000
-----							
2	Mg1	Mg	1.00000	0.90820	0.25000	2.378	2.000

Output Comment

Press "Del" to delete selected objects, "Esc" to reset deleted objects.

K. Momma and F. Izumi, VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data, *J. Appl. Cryst.* **44** (2011) 1272–1276.  
[doi:10.1107/S0021889811038970]

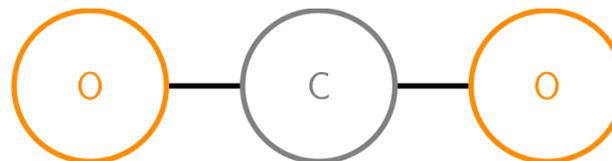
## Crystal structures of simple oxides [containing a single cation site]

# Crystal structures of simple oxides [containing a single cation site]

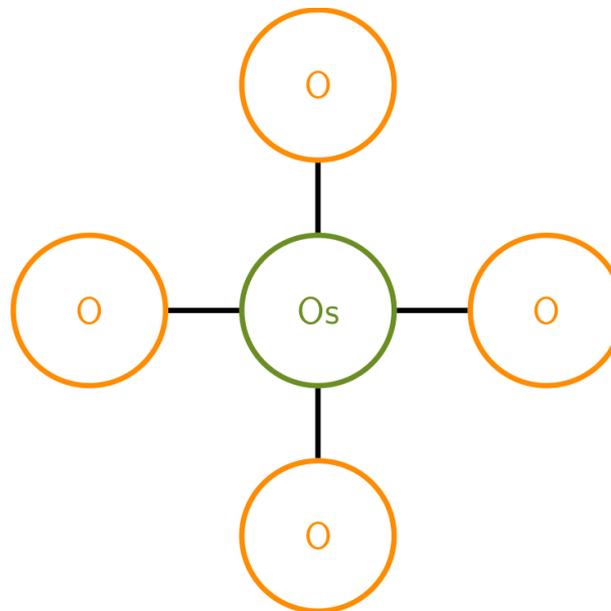
N.B.: CoO is simple,  $\text{Co}_3\text{O}_4$  is not.  $\text{ZnCo}_2\text{O}_4$  is certainly not!  
 $\text{Co}_3\text{O}_4$  and  $\text{ZnCo}_2\text{O}_4$  are complex oxides.

**Graphs** of connectivity in crystals: Atoms are nodes and edges (the lines that connect nodes) indicate short (near-neighbor) distances.

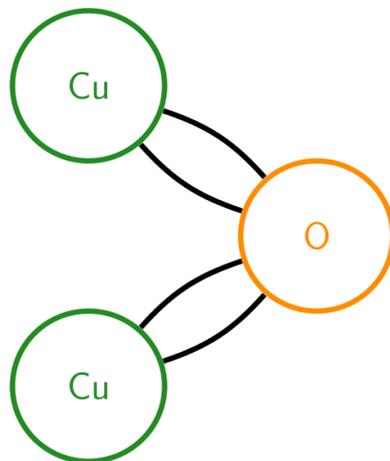
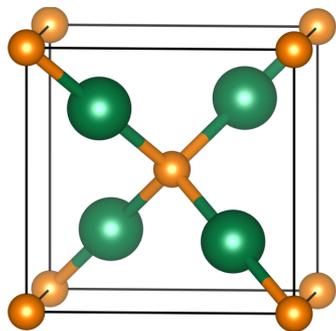
$\text{CO}_2$ : The molecular structure is  $\text{O}=\text{C}=\text{O}$ . The graph is:  
Each C connected to 2 O, each O connected to a 1 C



$\text{OsO}_4$ : The structure comprises isolated tetrahedra (molecular). The graph is below:  
Each Os connected to 4 O and each O to 1 Os

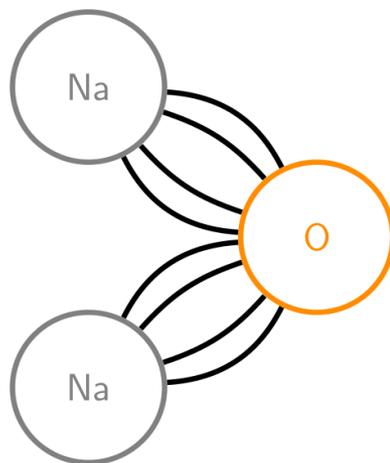
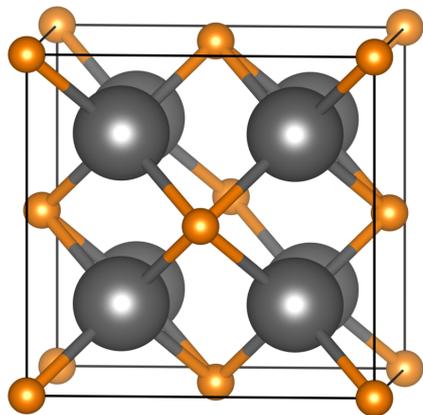


$Cu_2O$



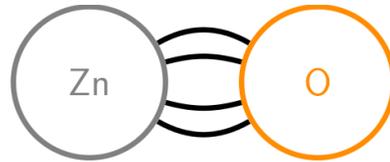
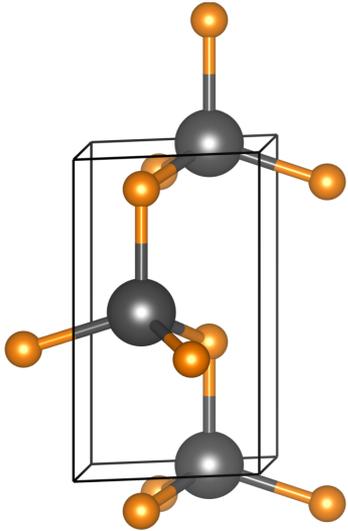
Linear coordination is unusual. Found usually in  $Cu^+$  and  $Ag^+$ .

$Na_2O$  (anti-fluorite)

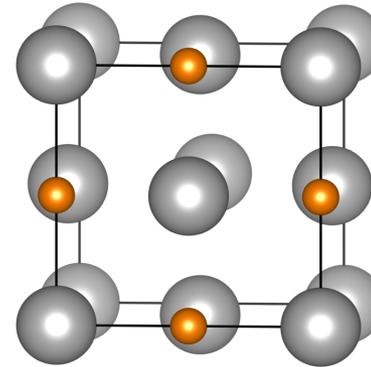


4-coordination for  $Na^+$  and 8-coordination for  $O^{2-}$  are unusual.

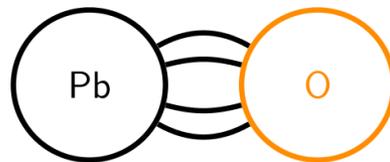
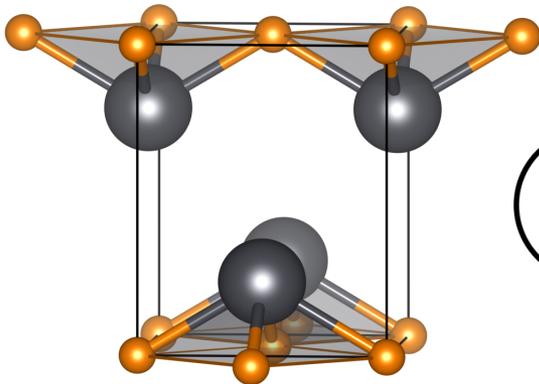
ZnO (wurtzite),  $sp^3$



MgO (rock-salt)



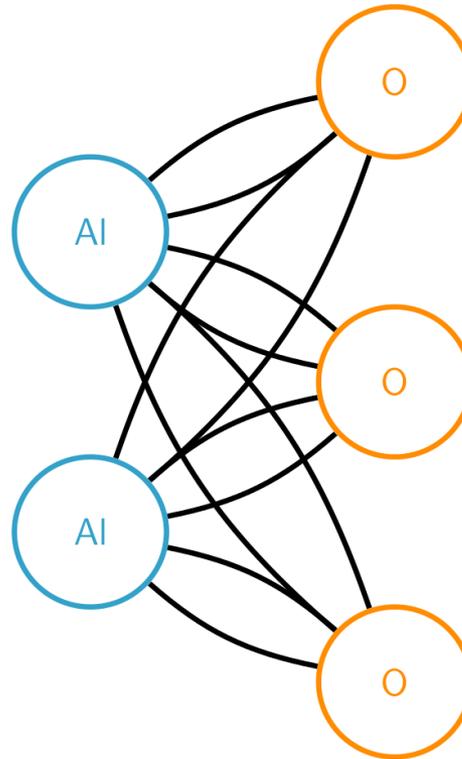
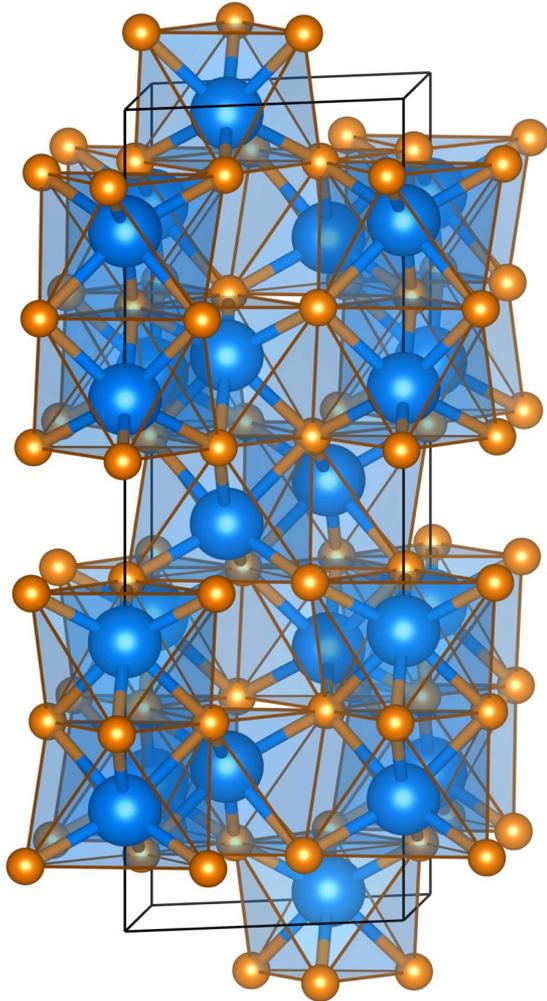
PbO (litharge), lone pairs



Ubiquitous for AO oxides including transition metals (distorted for CuO and NbO).

Insulators, metals (TiO), magnetic, ...

$\alpha\text{-Al}_2\text{O}_3$  (corundum)

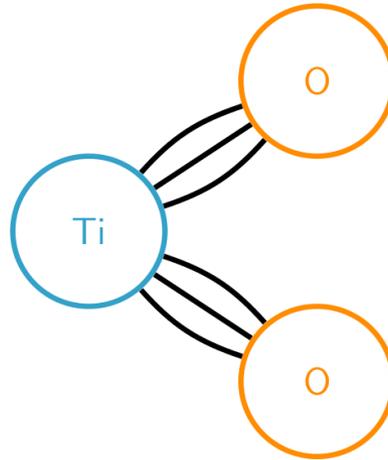
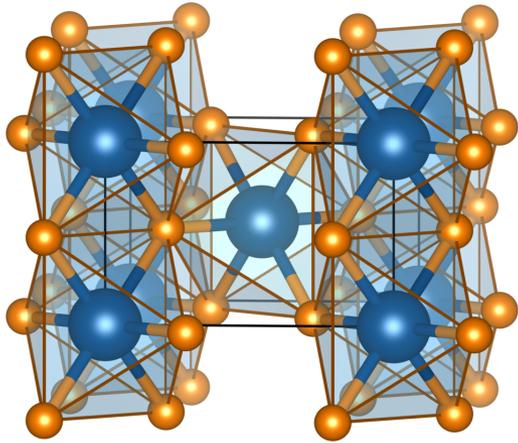


Also the structure of  $\text{Cr}_2\text{O}_3$   
and  $\text{Fe}_2\text{O}_3$ .

$\text{Ga}_2\text{O}_3$  does funny things.

$\text{In}_2\text{O}_3$  is different (bixbyite).

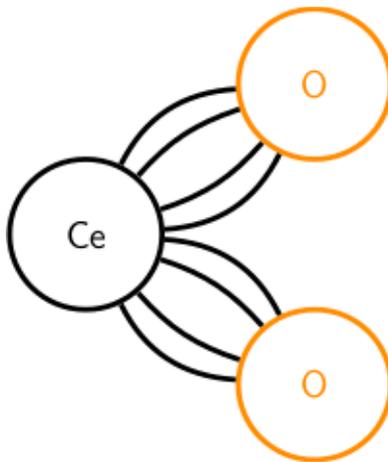
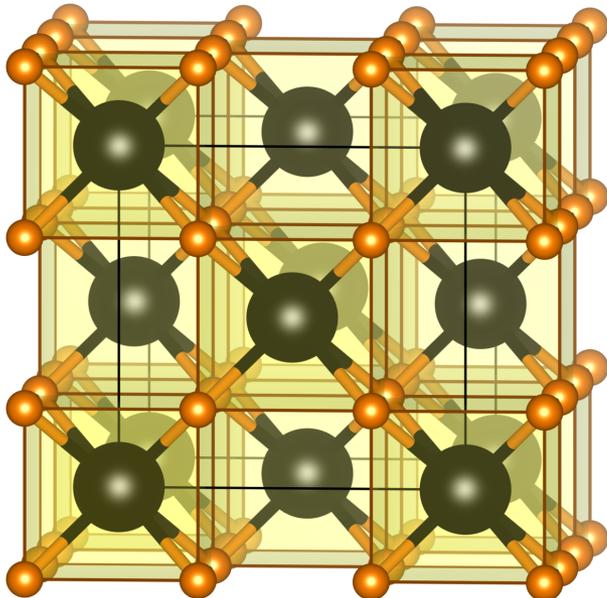
### $\text{TiO}_2$ (rutile)



$\text{TiO}_2$  also crystallizes as anatase and brookite.

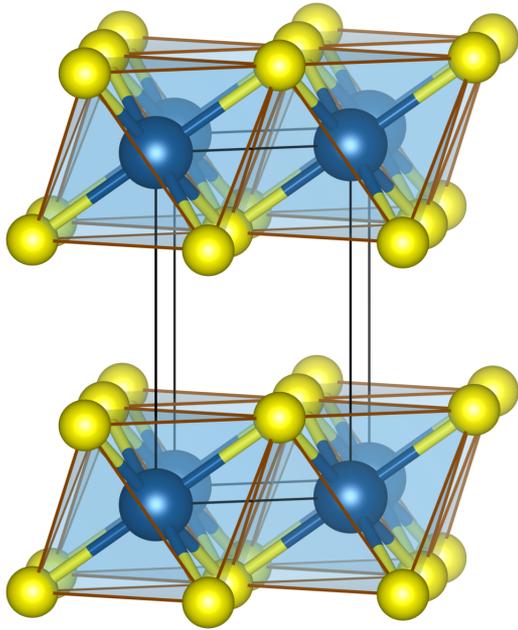
$\text{SiO}_2$  takes on this structure, and can be quenched to it, (stishovite) under pressure.

### $\text{CeO}_2$ (fluorite)



Also the structure of  $\text{ThO}_2$ , and of  $\text{ZrO}_2$  and  $\text{HfO}_2$  at elevated temperatures.

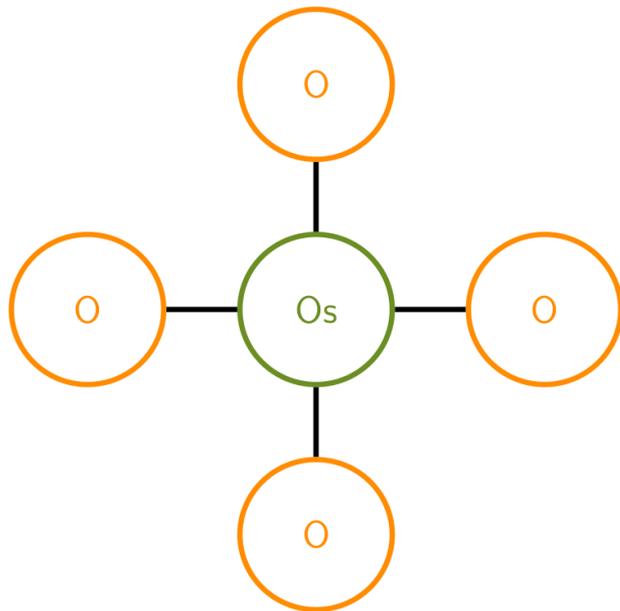
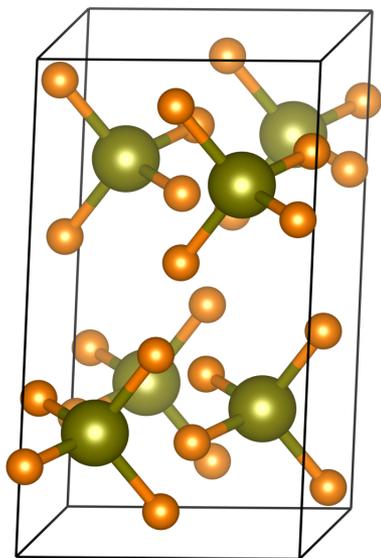
Ordered variants abound.



van der Waals gap (unlikely in oxides or fluorides, but occurs frequently in hydroxides)

This is the  $\text{CdI}_2$  structure.

$\text{OsO}_4$



# Shannon-Prewitt (ionic) radii

Radii assigned by systematically examining cation-anion pairs in oxides, fluorides etc.

May not work for other kinds of compounds

Be sensitive to coordination number and spin state

Ram Seshadri Group at UCSB: Periodic Table

www.mrl.ucsb.edu/~seshadri/Periodic/index.html

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Compute with Wolfram|Alpha

### Periodic table of the elements

Click on the element for tables of the Effective Ionic Radii

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
H 1 1.008																	He 2 4.003
Li 3 6.941	Be 4 9.012											B 5 10.81	C 6 12.01	N 7 14.01	O 8 16.00	F 9 19.00	Ne 10 20.18
Na 11 22.99	Mg 12 24.30											Al 13 26.98	Si 14 28.09	P 15 30.97	S 16 32.07	Cl 17 35.45	Ar 18 39.95
K 19 39.10	Ca 20 40.08	Sc 21 44.96	Ti 22 47.88	V 23 50.94	Cr 24 52.00	Mn 25 54.94	Fe 26 55.85	Co 27 58.93	Ni 28 58.69	Cu 29 63.55	Zn 30 65.39	Ga 31 69.72	Ge 32 72.61	As 33 74.92	Se 34 78.96	Br 35 79.90	Kr 36 83.80
Rb 37 85.47	Sr 38 87.62	Y 39 88.91	Zr 40 91.22	Nb 41 92.91	Mo 42 95.94	Tc 43 98.91	Ru 44 101.1	Rh 45 101.1	Pd 46 106.4	Ag 47 107.9	Cd 48 112.4	In 49 114.8	Sn 50 118.7	Sb 51 121.8	Te 52 127.6	I 53 126.9	Xe 54 131.3
Cs 55 132.9	Ba 56 137.3	La 57 138.9	Hf 72 178.5	Ta 73 180.9	W 74 183.8	Re 75 186.2	Os 76 190.2	Ir 77 192.2	Pt 78 195.1	Au 79 197.0	Hg 80 200.6	Tl 81 204.4	Pb 82 207.2	Bi 83 209.0	Po 84 210.0	At 85 210.0	Rn 86 222.0
Fr 87 223.0	Ra 88 226.0	Ac 89 227.0															
		Ce 58 140.1	Pr 59 140.9	Nd 60 144.2	Pm 61 144.9	Sm 62 150.4	Eu 63 152.0	Gd 64 157.2	Tb 65 158.9	Dy 66 162.5	Ho 67 164.9	Er 68 167.3	Tm 69 168.9	Yb 70 173.0	Lu 71 175.0		
		Th 90 232.0	Pa 91 231.0	U 92 238.0	Np 93 237.0	Pu 94 239.1	Am 95 243.1	Cm 96 247.1	Bk 97 247.1	Cf 98 252.1	Es 99 252.1	Fm 100 257.1	Md 101 256.1	No 102 259.1	Lr 103 260.1		

### Mn

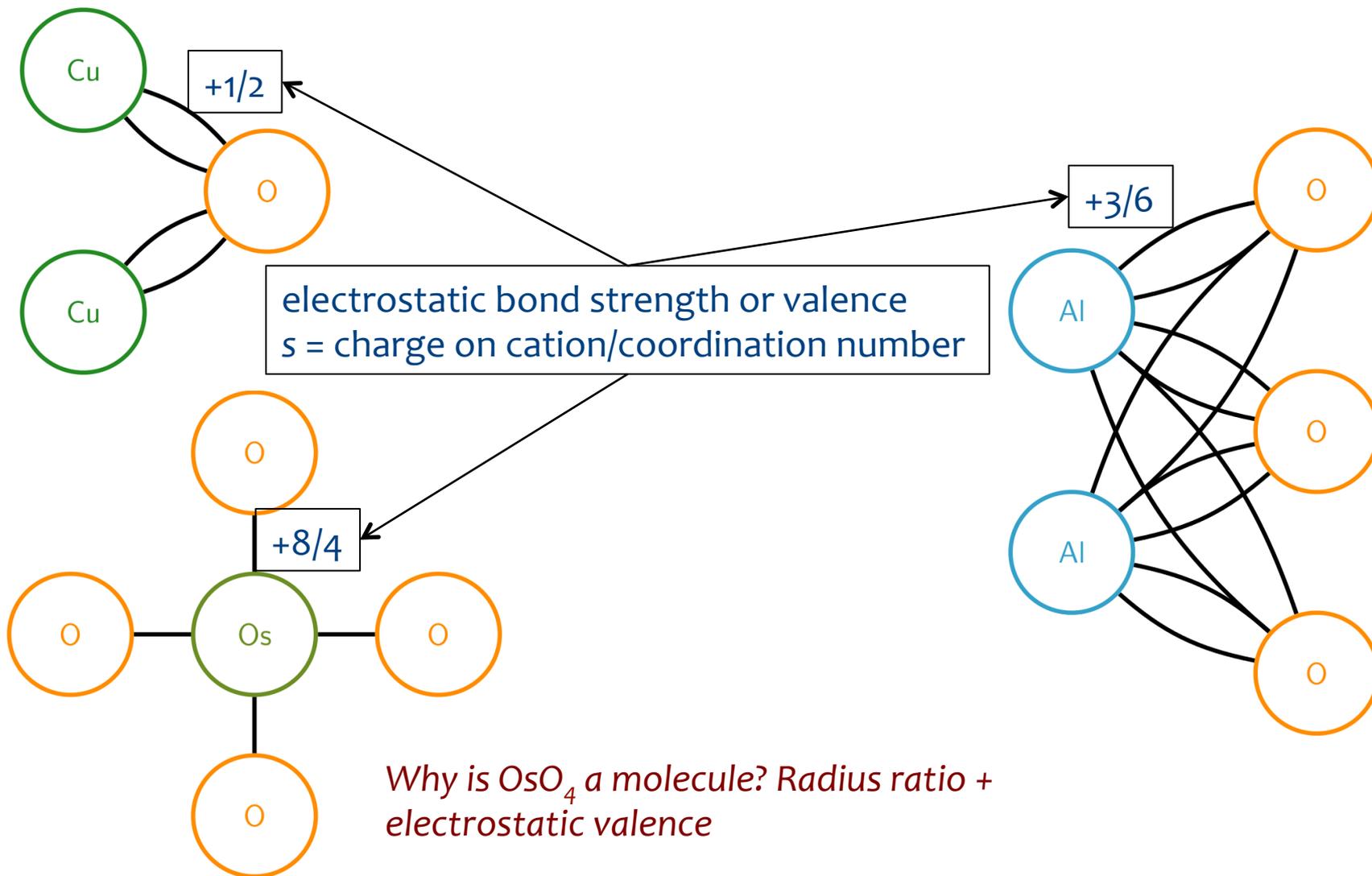
Charge	C.N.	Spin	I.R./Å
+2	4	h	0.66
	5	h	0.75
	6	l	0.67
	6	h	0.830
	7	h	0.90
	8		0.96
+3	5		0.58
	6	l	0.58
	6	h	0.645
+4	4		0.39
	6		0.530
+5	4		0.33
+6	4		0.255
+7	4		0.25
	6		0.46

## Ionic radii and Pauling's first rule (the radius ratio rule)

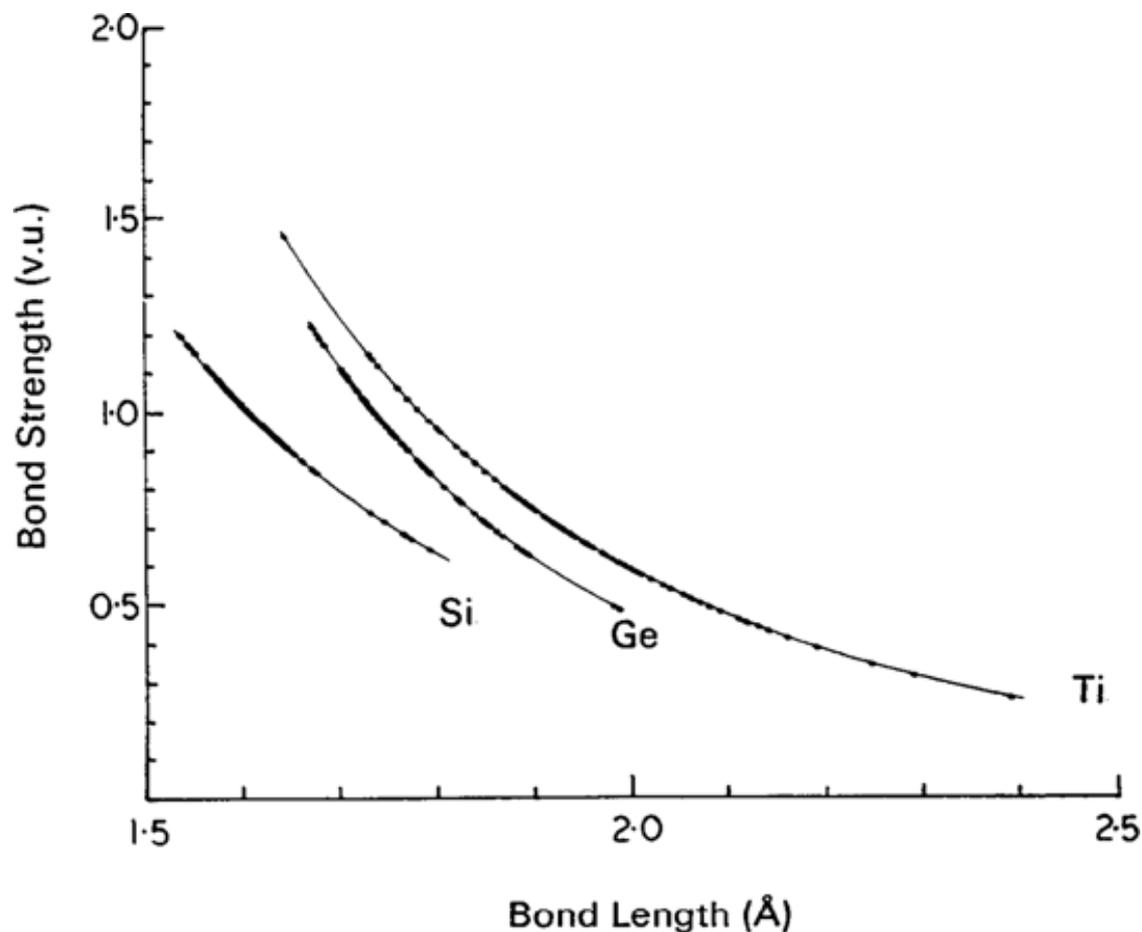
In brief: The cation-anion distance is the sum of cation and anion radii, and the number of anions around a cation (the coordination number) is a function of the radius ratio. Exemplified by  $\text{AO}_2$  compounds below. MRR is the minimum radius ratio.

Compound	$r_C$ (Å)	$r_C + r_O$ (Å)	$r_C/r_O$	Coordination	MRR
$\text{CO}_2$	-0.19(?)	1.16 (exp.)	?	2	
$\text{SiO}_2$	0.26	1.61	0.19	4	0.225
$\text{TiO}_2$	0.605	1.955	0.45	6	0.414
$\text{CeO}_2$	0.97	2.32	0.72	8	0.732

In brief: Charges going out from cations should balance anions and vice-versa



Pauling, and later Brown and Shannon, noted that the Pauling bond strength (the electrostatic valence) correlates very well with distance for many oxides: Short bonds (distances) correspond to strong bonds and vice-versa

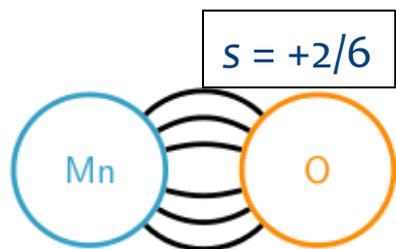


The modern bond valence relationship:

$$s = \exp\left(\frac{R_0 - R}{B}\right)$$

Where  $s$  is the strength of the bond,  $R$  is the cation to anion distance, and  $R_0$  and  $B \approx 0.37 \text{ \AA}$  are parametrized for the specific ion pair.

When all  $s$  are calculated:  $\sum_{\text{CN}} s = \text{valence of the ion}$



For  $\text{Mn}^{2+}-\text{O}^{2-}$ ,  $R_0 = 1.790 \text{ \AA}$ ,  $B = 0.37 \text{ \AA}$ .

This means  $R = 2.20 \text{ \AA}$ .  
experiment:  $2.22 \text{ \AA}$

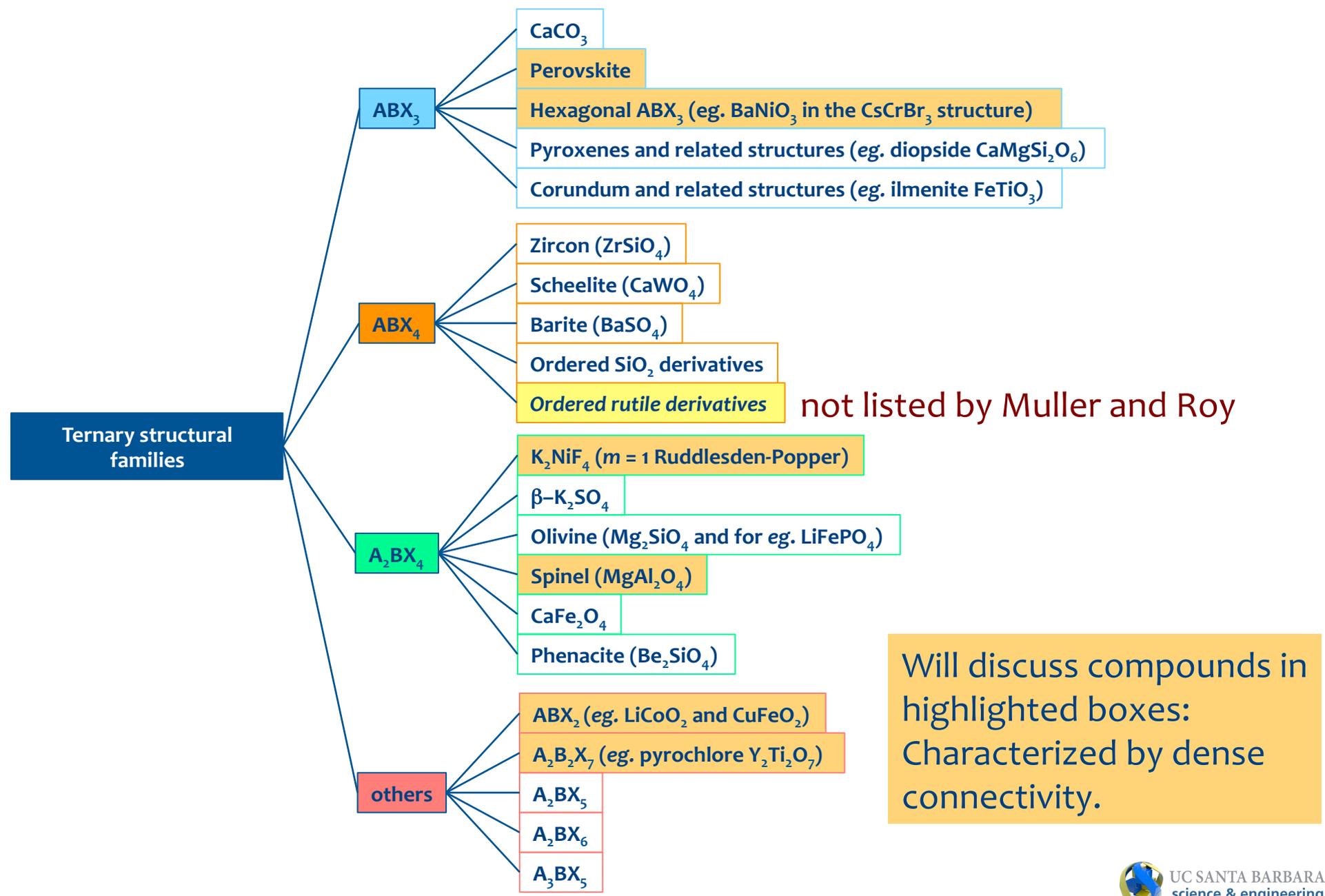
# Electrostatic valence and bond valence: Parameters for Mn

Mn 2	0	-2	1.790	0.37	a
Mn 2	0	-2	1.765	0.37	j
Mn 2	S	-2	2.22	0.37	e
Mn 2	F	-1	1.698	0.37	a
Mn 2	Cl	-1	2.133	0.37	a
Mn 2	Br	-1	2.34	0.37	e
Mn 2	I	-2	2.52	0.37	e
Mn 2	N	-3	1.849	0.37	j
<b>Mn 2</b>	<b>N</b>	<b>-3</b>	<b>1.65</b>	<b>0.35</b>	<b>e</b>
Mn 3	0	-2	1.760	0.37	a
Mn 3	0	-2	1.732	0.37	j
Mn 3	F	-1	1.66	0.37	b
Mn 3	Cl	-1	2.14	0.37	b
Mn 3	N	-3	1.837	0.37	j
Mn 4	0	-2	1.753	0.37	a
Mn 4	0	-2	1.750	0.37	j
Mn 4	F	-1	1.71	0.37	b
Mn 4	F	-1	1.63	0.37	e
Mn 4	Cl	-1	2.13	0.37	b
Mn 4	N	-3	1.822	0.37	j
Mn 6	0	-2	1.79	0.37	e
Mn 7	0	-2	1.827	0.37	e
Mn 7	0	-2	1.79	0.37	b
Mn 7	F	-1	1.72	0.37	b
Mn 7	Cl	-1	2.17	0.37	b

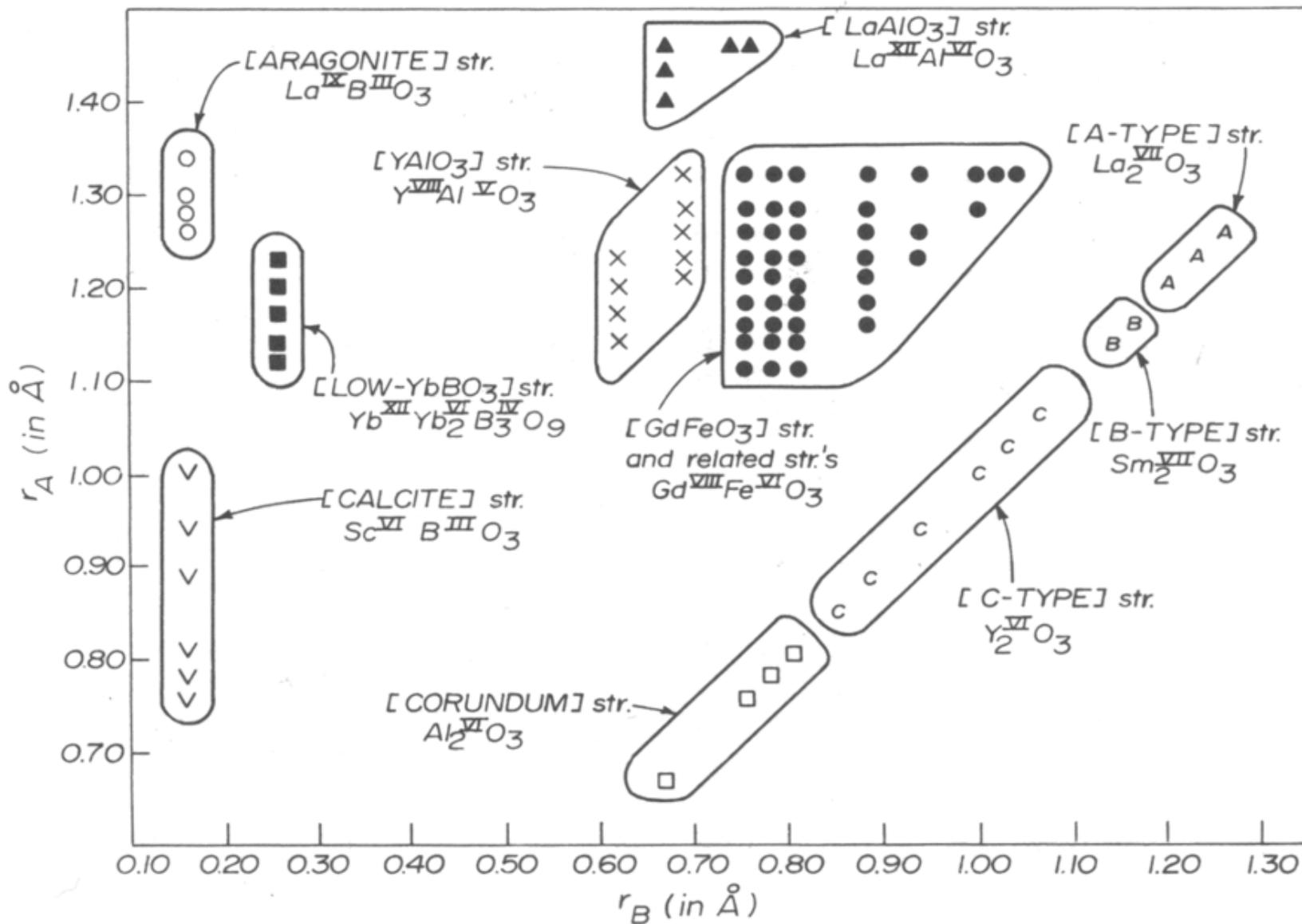
bvsparm.cif

## Crystal structures of some complex oxides [containing two or more cation sites]

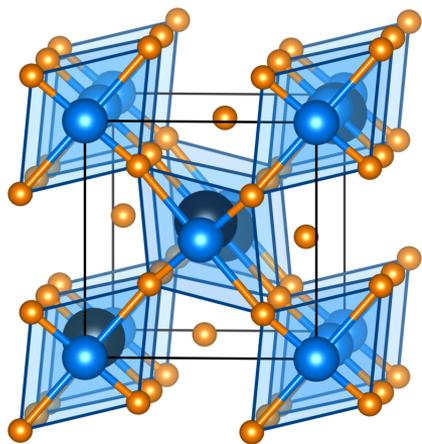
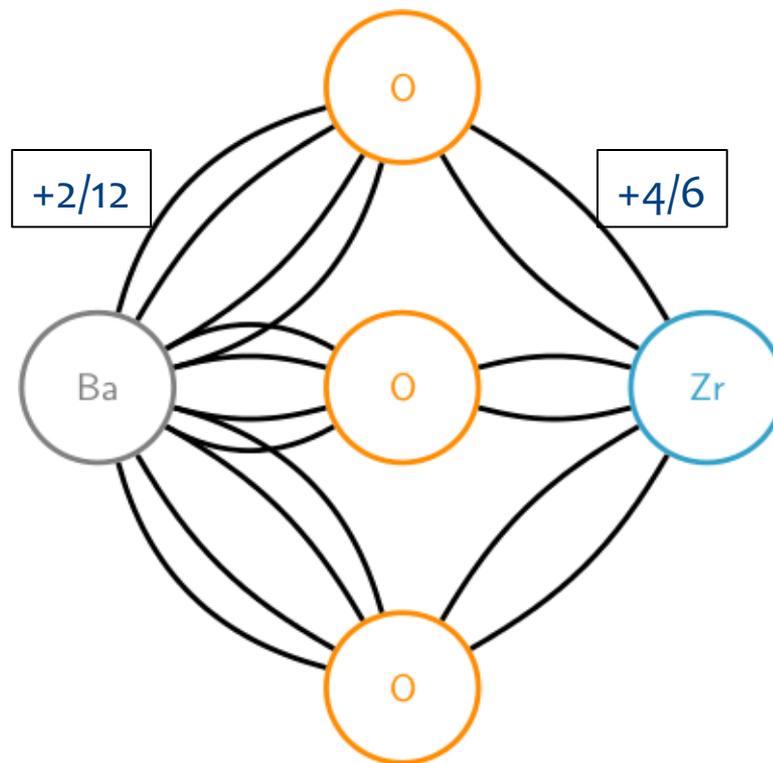
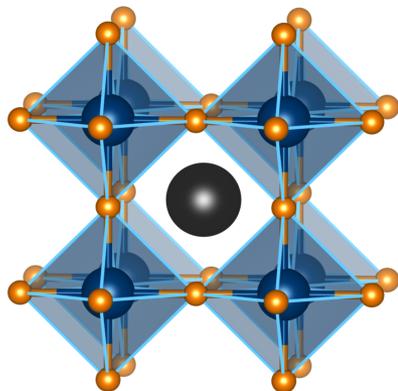
# The major ternary structural families (Muller and Roy, page 3, redrawn and modified)



# The $ABO_3$ structure-sorting field (from Muller and Roy)



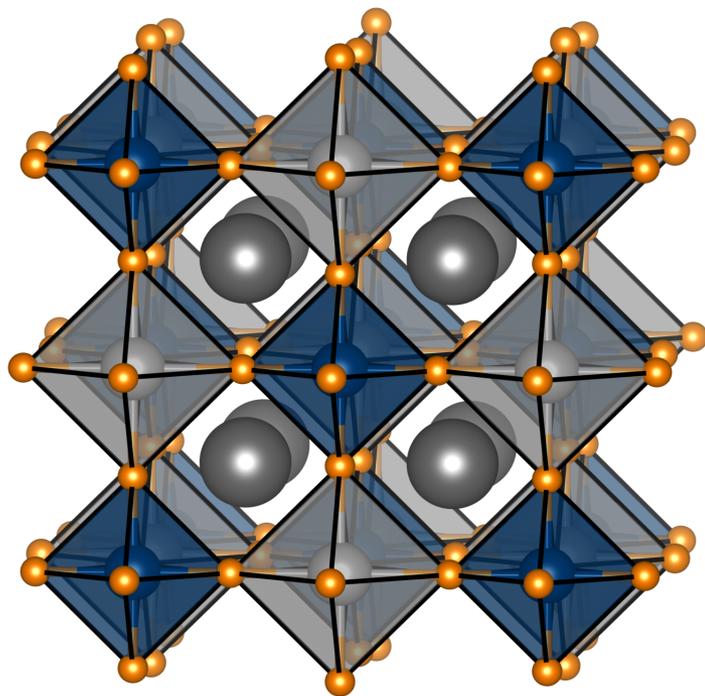
The superscripted roman numerals indicate coordination number.



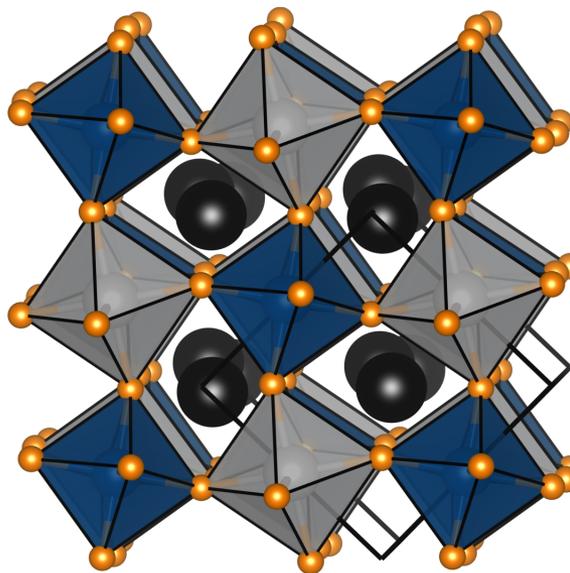
Note that the space group *Pnma* (#62) can be written in a variety of ways.

This is the most common perovskite space group.

In the next so many structures,  $\text{BO}_6$ -polyhedra are depicted.

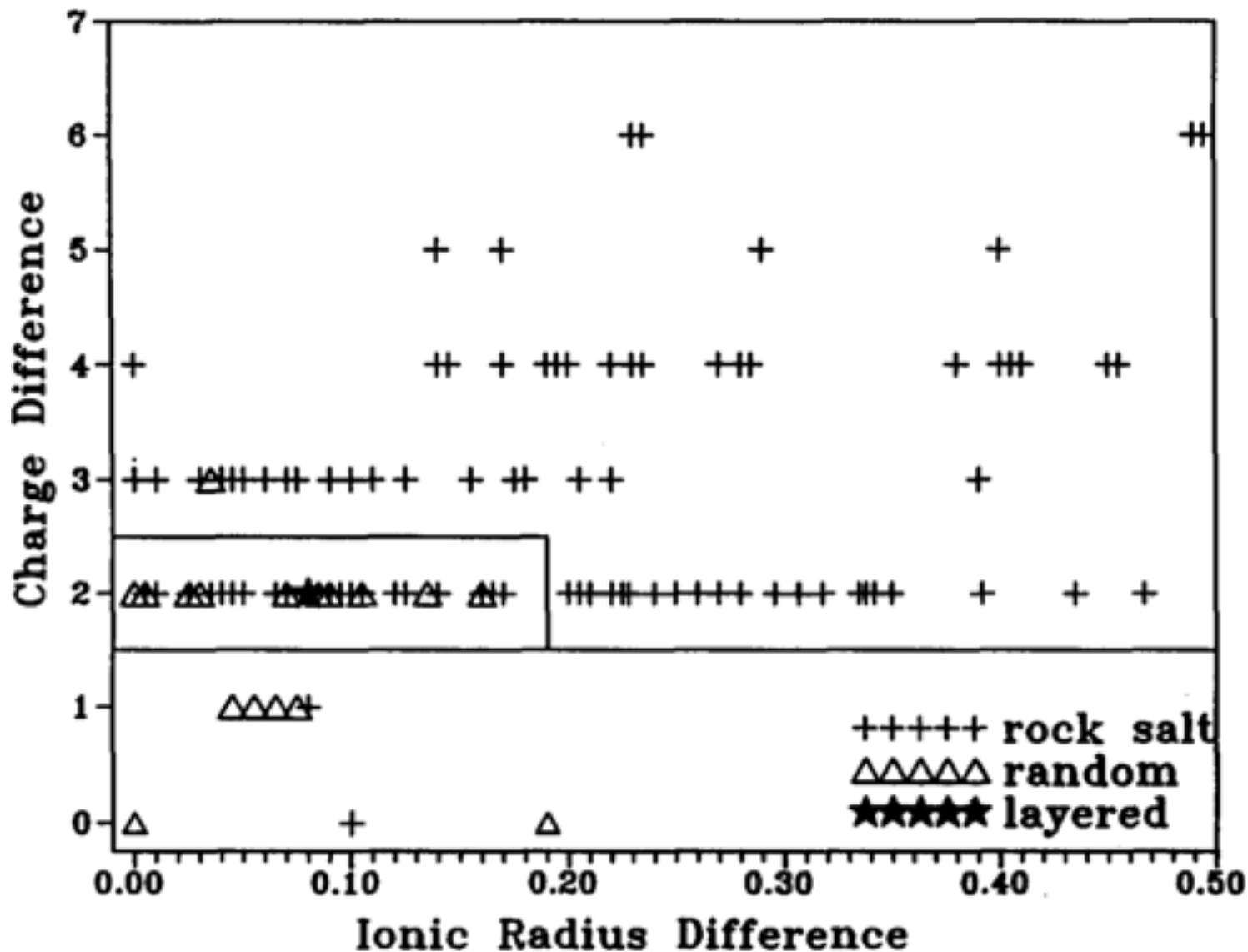


Rock-salt like ordering of dissimilar octahedra. Space group same as rock-salt:  $Fm\bar{3}m$

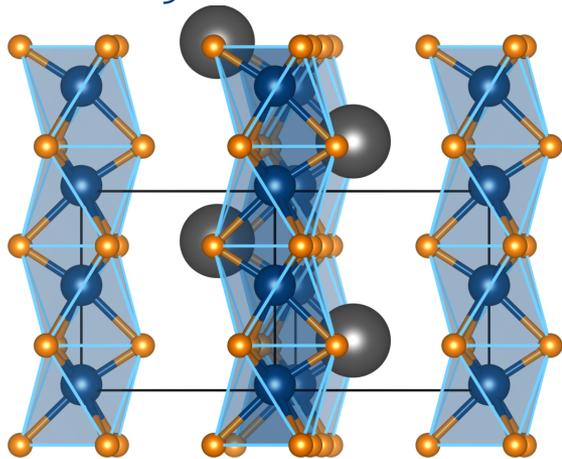


Smaller A-ions associated with tilting as in simple perovskites.

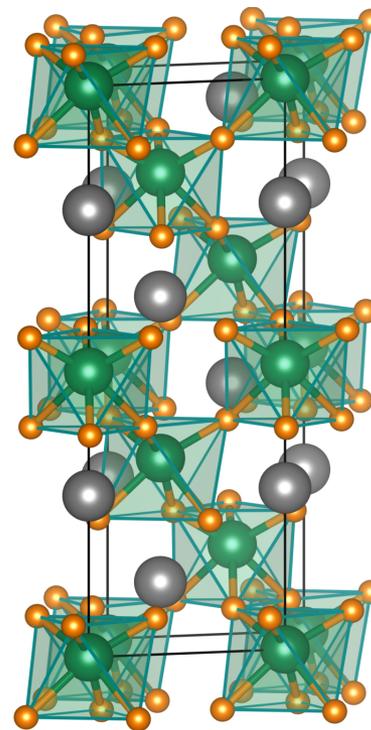
# The double perovskite field: Charge and radius



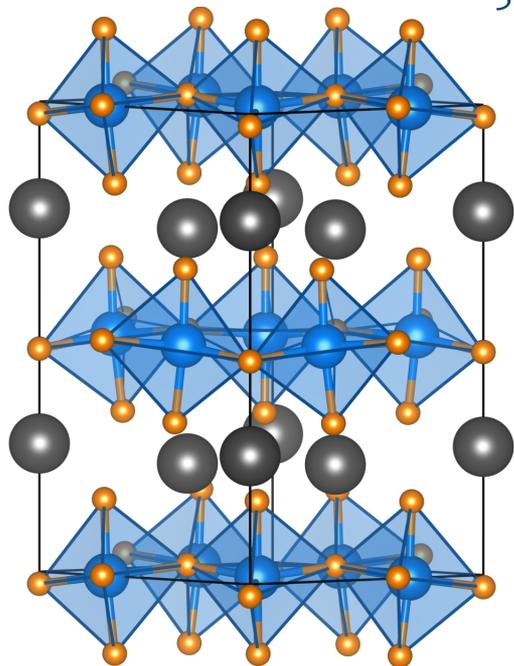
$BaNiO_3$



$LiNbO_3$  (ferroelectric  $R3c$ )

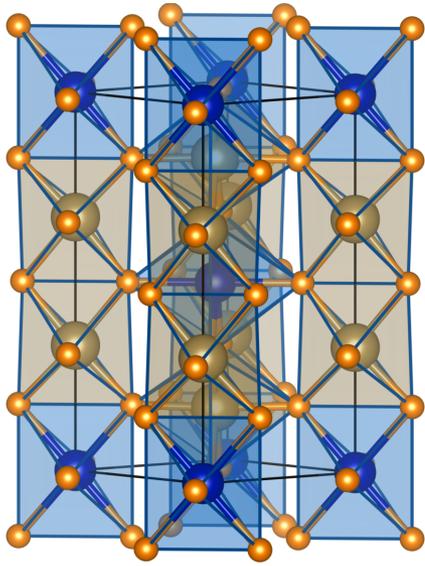


Ferroelectric  $YMnO_3$  (“ $YAlO_3$ ”)

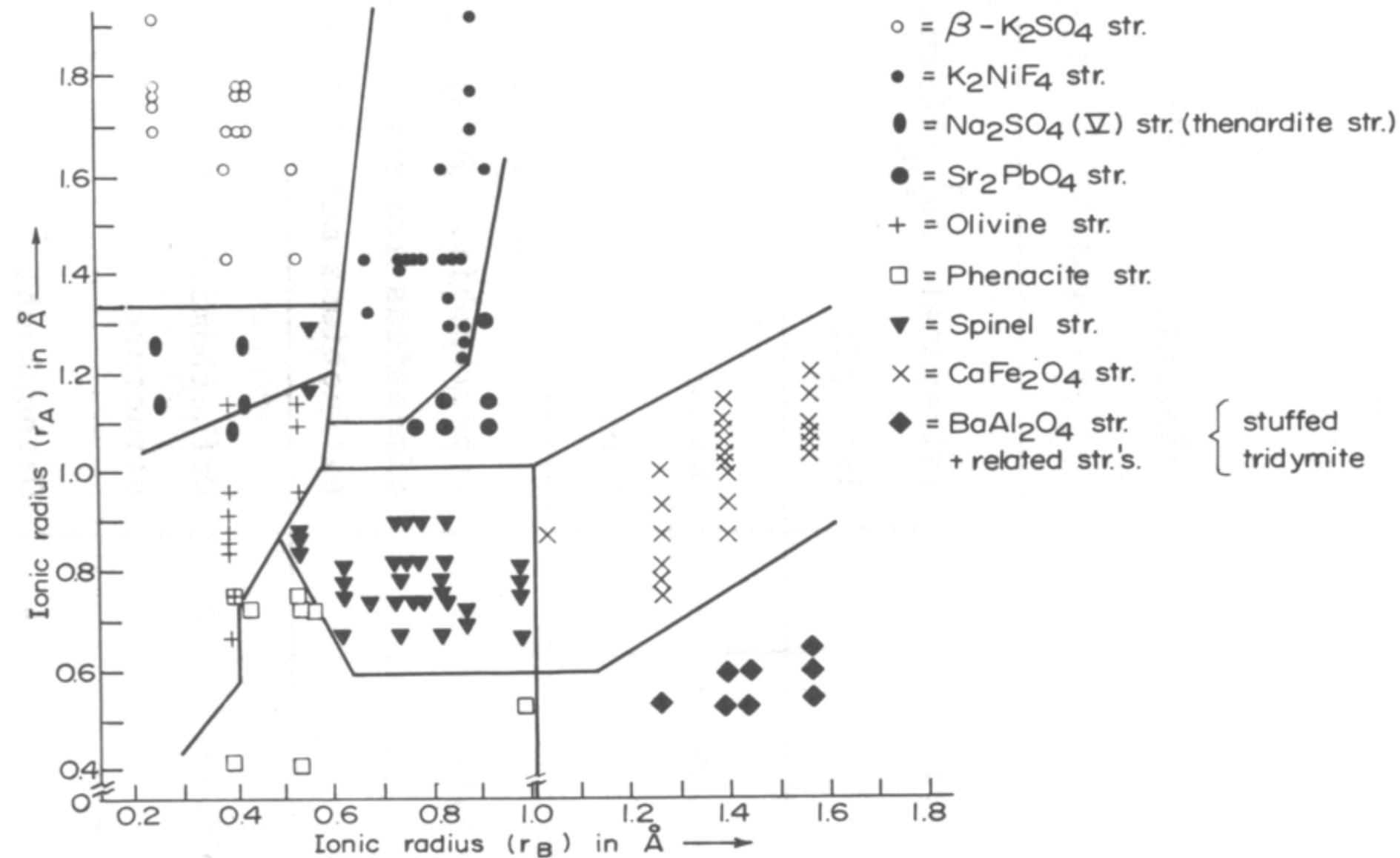


Unusual 5-fold coordination  
(trigonal bipyramid) of  $MnO_5$

# Ordered rutiles (the trirutile)

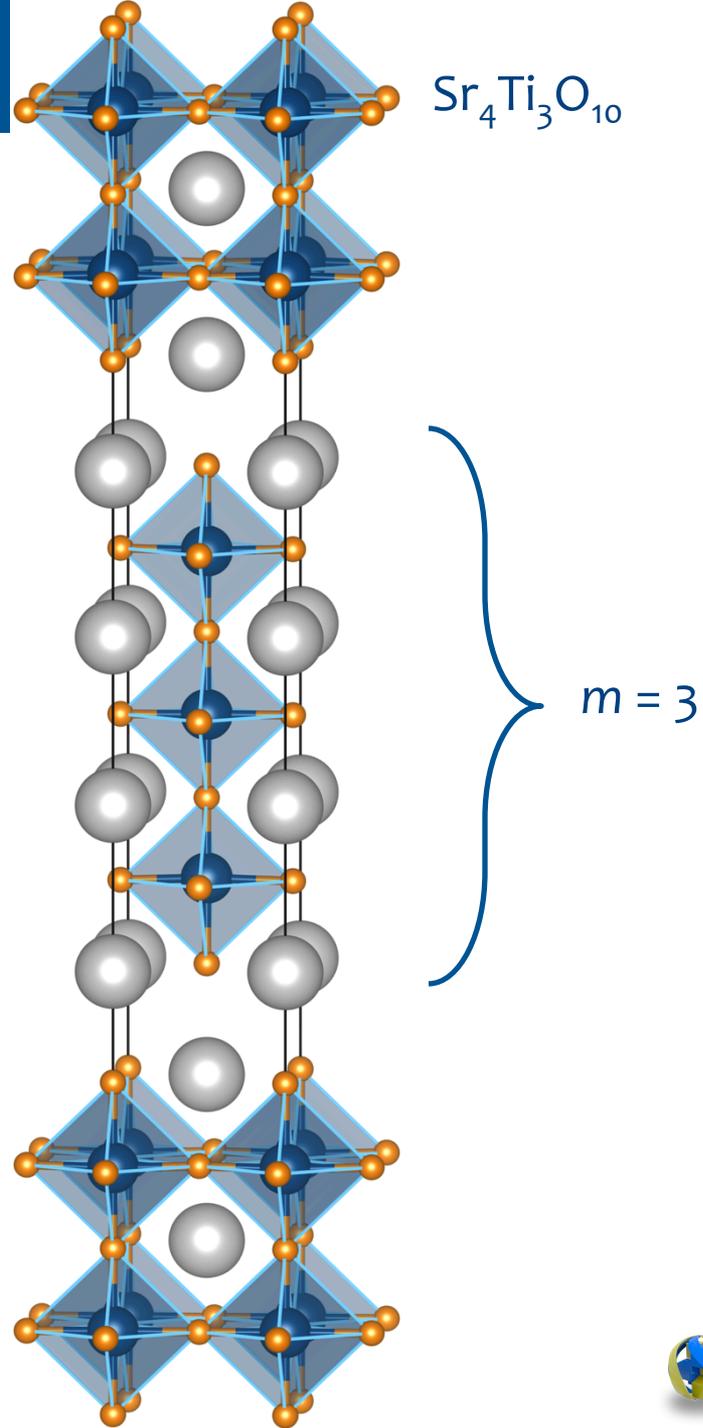
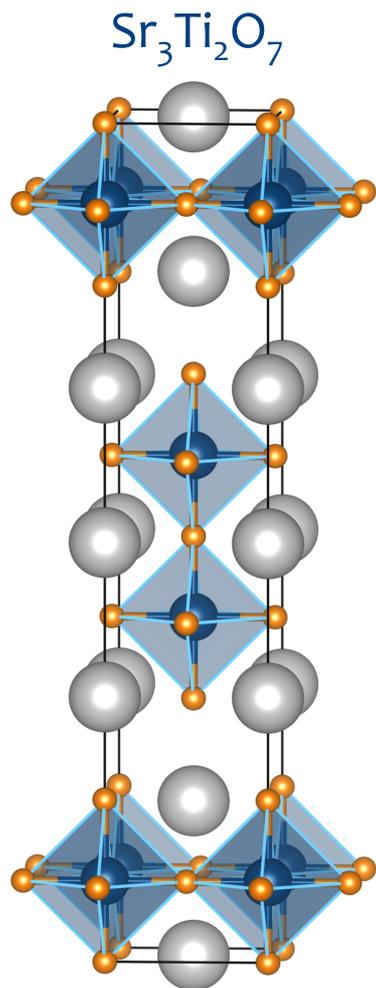
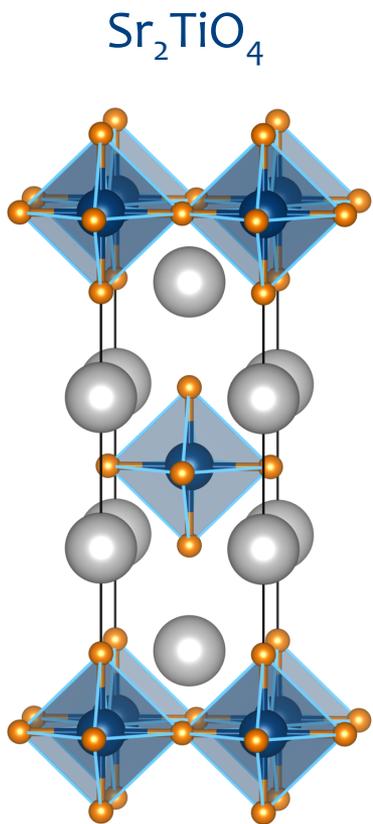


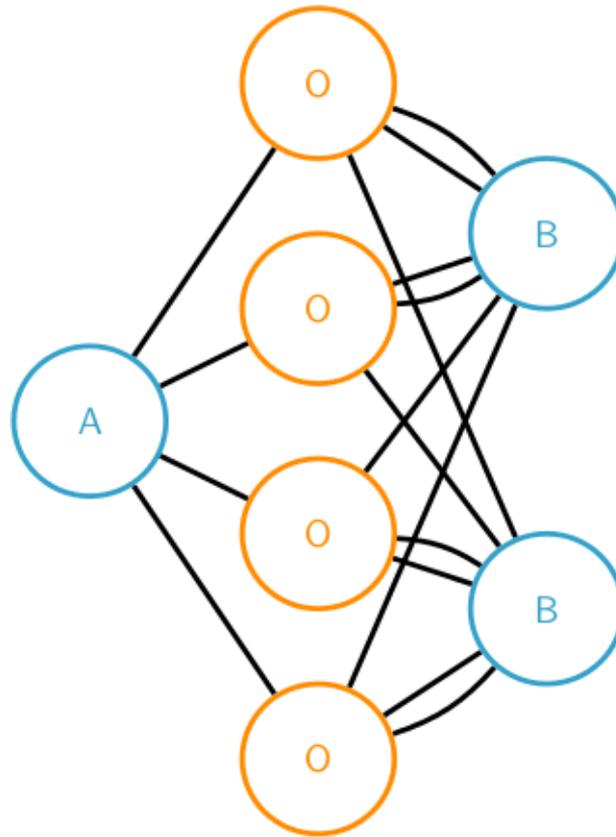
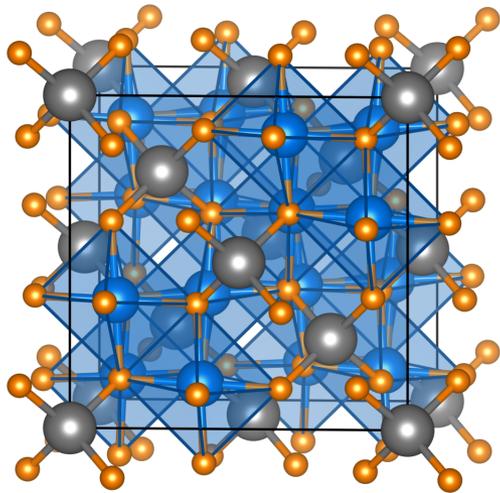
# The $A_2BO_4$ structure-sorting field (from Muller and Roy)



The superscripted roman numerals indicate coordination number.

$K_2NiF_4$  and Ruddlesden-Popper ( $m = 1, 2, 3$ )  
General formula  $[SrO][SrTiO_3]_m$





Ubiquitous structure when ions have similar sizes, around  $0.6 \text{ \AA}$ .  
A is tetrahedrally coordinated, and B octahedral (actually with a slight trigonal distortion).

In general, lower oxidation states and smaller bandwidths than in perovskites.

ions on the A site

Li														
	Mg												Al	
		Sc	Ti	V	Cr	Mn I	Fe III	Co II	Ni	Cu	Zn	Ga	Ge	
								Rh		Ag	Cd	In	Sn	

ions on the B site

Li														
	Mg												Al	
		Sc	Ti III	V III	Cr III	Mn II	Fe II,III	Co II	Ni II	Cu	Zn	Ga	Ge	
								Co, Rh III		Ag	Cd	In	Sn	



A,B Jahn-Teller active

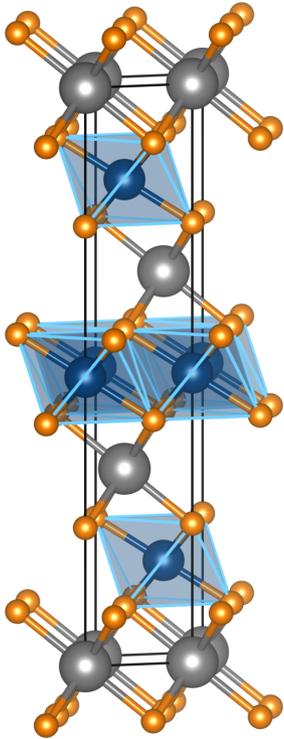


A,B Diamagnetic



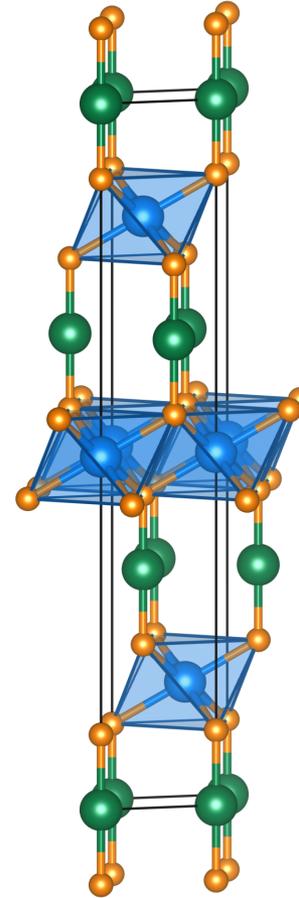
Co II High single-ion anisotropy

$LiCoO_2$  (ordered rock-salt)

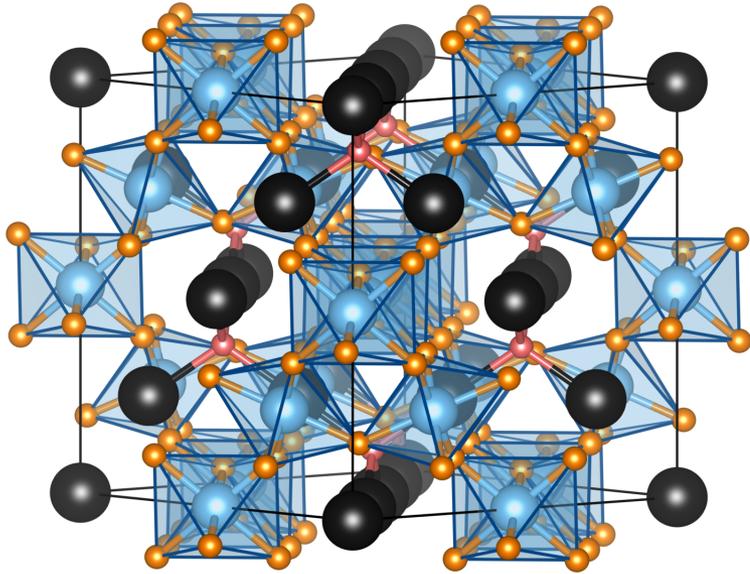


111-ordered with alternating octahedral  $LiO_6$  and  $CoO_6$  stacking

$3R-CuFeO_2$  (delafossite)

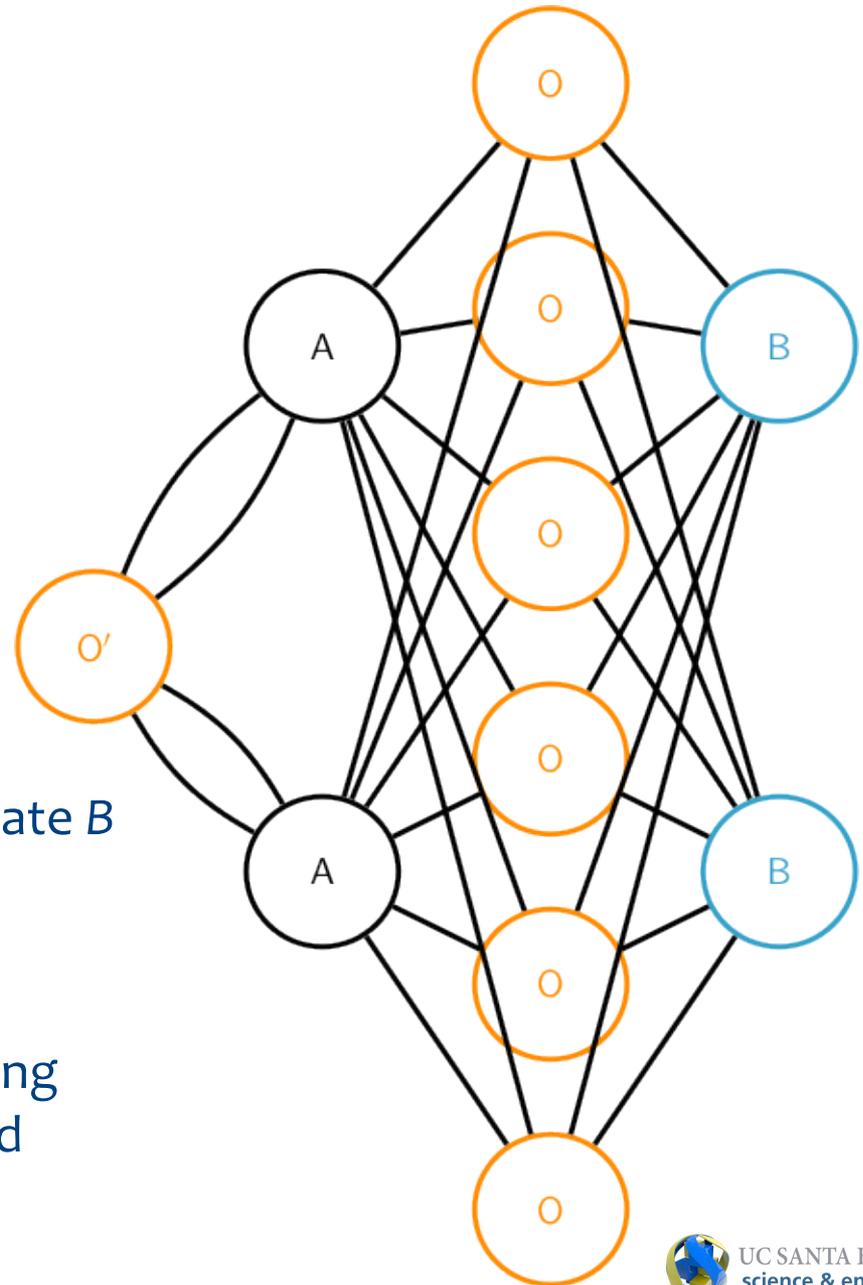


$BO_2$  ( $CdI_2$ ) slabs separated by two-coordinate atoms, usually  $Cu^+$  and  $Ag^+$ . Also unusually,  $Pd^{1+}$  and  $Pt^{1+}$ .



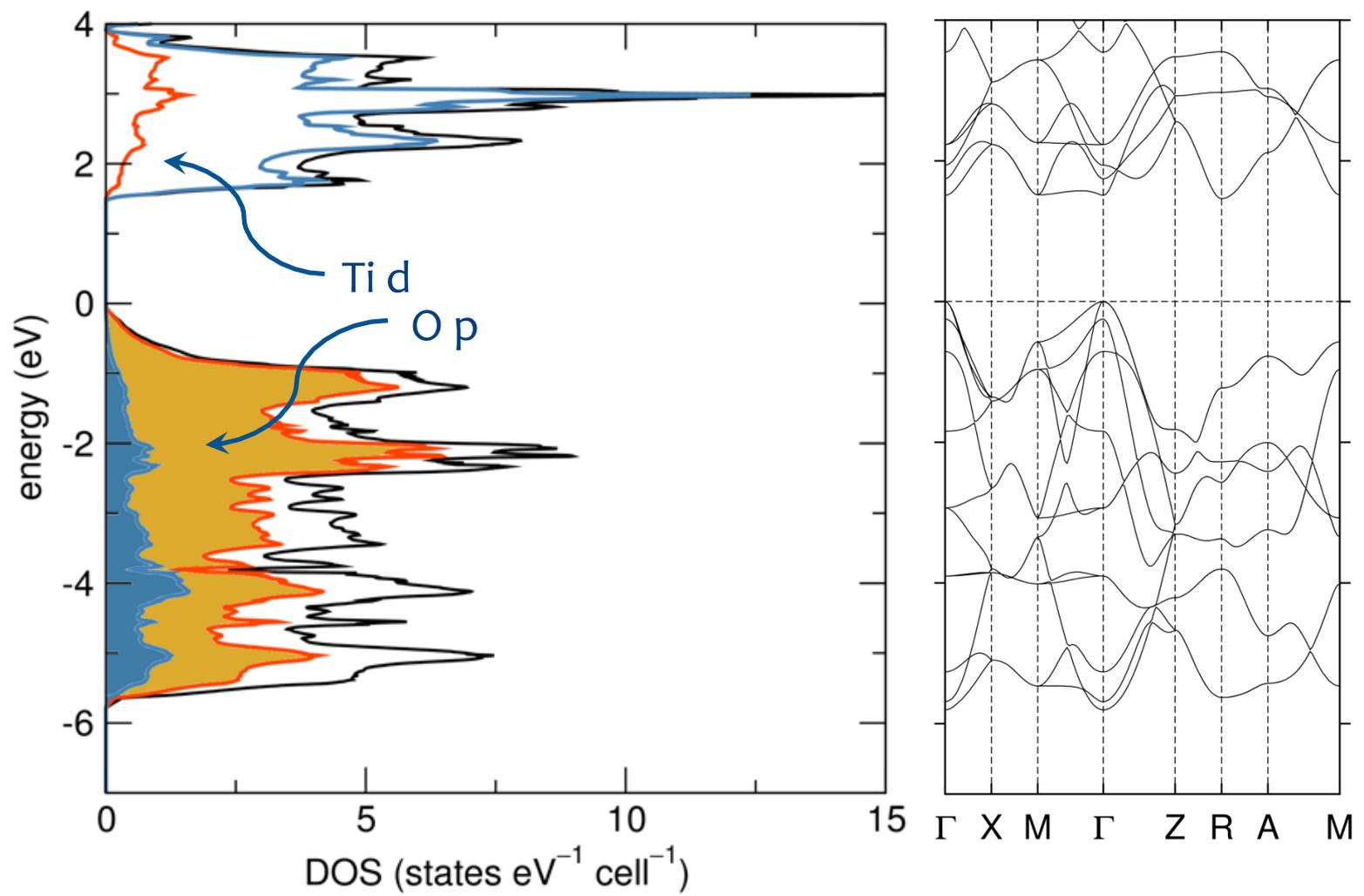
6+2-coordinate A atoms and 6-coordinate B atoms.

Separately, just connecting A or just connecting B yields two interpenetrating *pyrochlore* lattices of corner-connected tetrahedra.



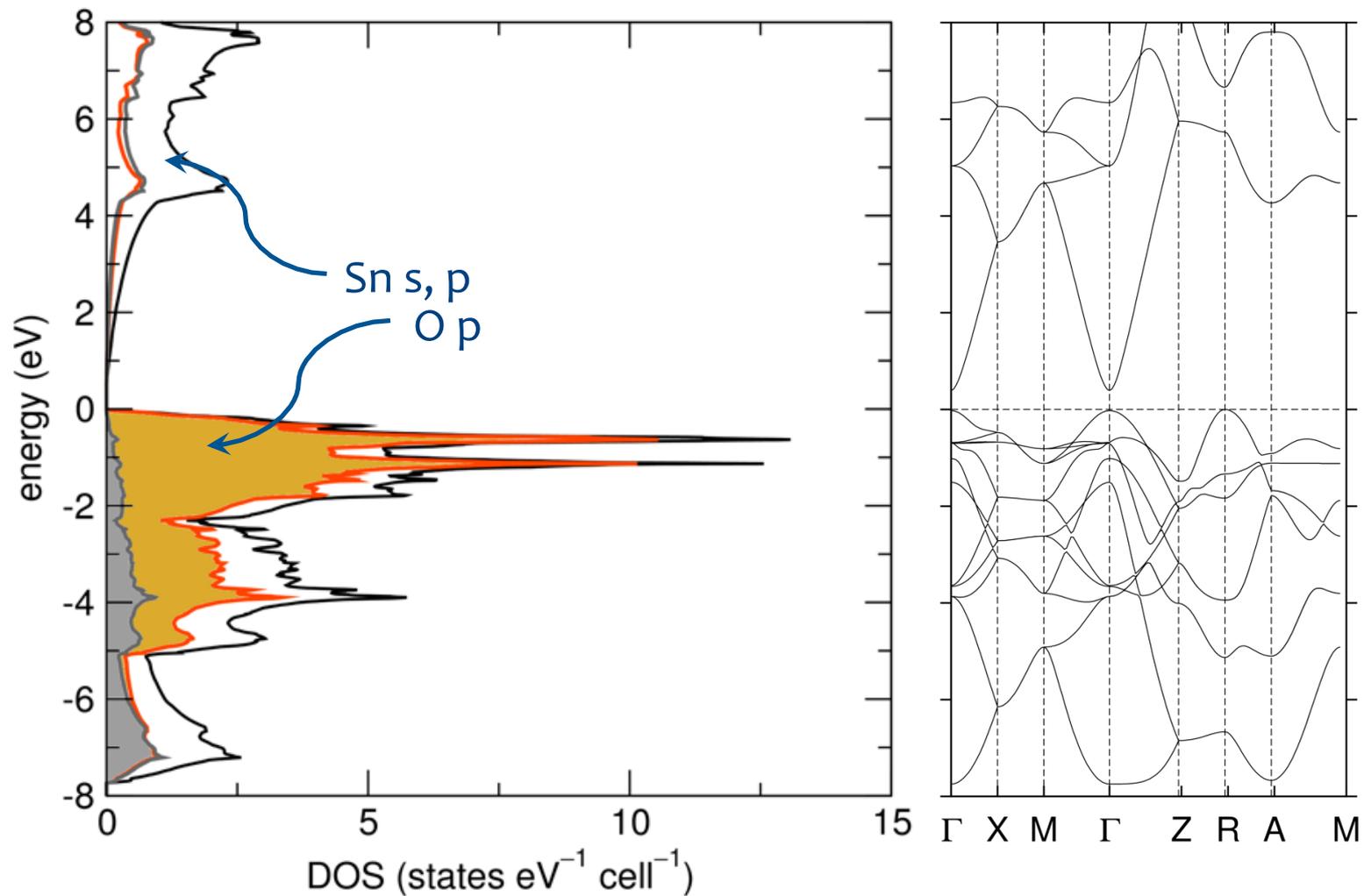
# Counting electrons

# Counting electrons in $\text{TiO}_2$ : Assign as $\text{Ti}^{4+}$ and $\text{O}^{2-}$



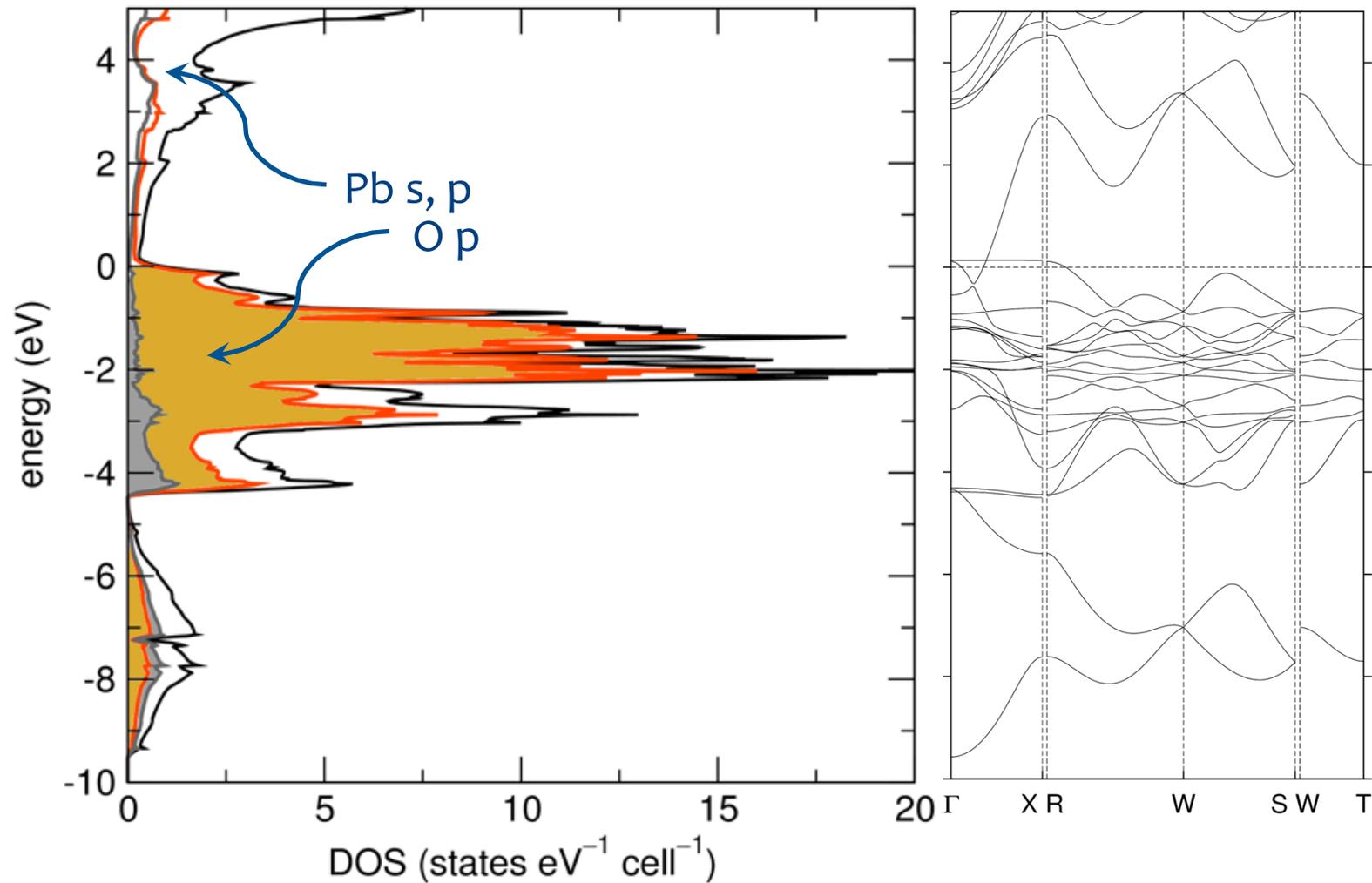
Insulator, not so easy to dope.

# Counting electrons in SnO<sub>2</sub>: Assign as Sn<sup>4+</sup> and O<sup>2-</sup> (more covalent than TiO<sub>2</sub>)



Insulator, easier to dope (TCOs).

# Counting electrons in $\text{BaPbO}_3$ : Assign as $\text{Pb}^{4+}$ and $\text{O}^{2-}$ . An unexpected semi-metal



Equivalent  $\text{Sn}^{4+}$  compounds are insulating.

## $d^0$ and $s^2$ systems: Second-Order Jahn-Teller (SOJT) effects

Expand the vibronic Hamiltonian in terms of a normal coordinate  $Q$  :

$$\mathcal{H} = \mathcal{H}^{(0)} + \mathcal{H}^{(1)}Q + \frac{1}{2}\mathcal{H}^{(2)}Q^2 + \dots$$

where:

$$\mathcal{H}^{(1)} = (\partial\mathcal{H}/\partial Q)_{Q=0}; \mathcal{H}^{(2)} = (\partial^2\mathcal{H}/\partial Q^2)_{Q=0}$$

resulting in:

$$E = E^{(0)} + \underbrace{\langle 0 | \mathcal{H}^{(1)} | 0 \rangle}_{1^{\text{st}} \text{ order (J-T)}} Q + \frac{1}{2} \underbrace{\left[ \langle 0 | \mathcal{H}^{(2)} | 0 \rangle - 2 \sum_n \frac{\langle 0 | \mathcal{H}^{(1)} | n \rangle^2}{E^{(n)} - E^{(0)}} \right]}_{\text{SOJT}} Q^2 + \dots$$

1<sup>st</sup> order (J-T)

SOJT

Seen in early transition metal oxides in their highest oxidation state. Effects strengthens with smaller ions and higher charge (*ie.* with higher covalency):

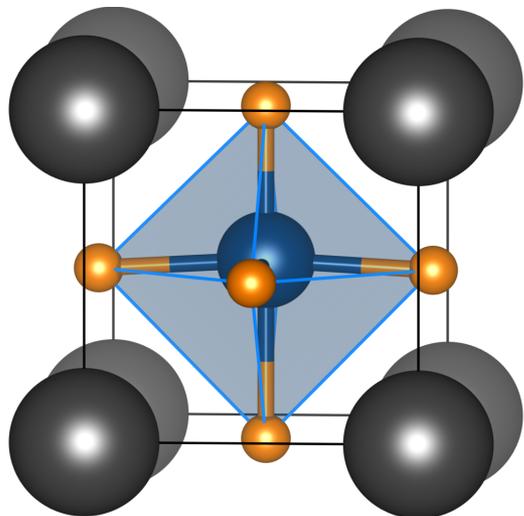
Sc <sup>3+</sup>	Ti <sup>4+</sup>	V <sup>5+</sup>	Cr <sup>6+</sup>
	Zr <sup>4+</sup>	Nb <sup>5+</sup>	Mo <sup>6+</sup>
	Hf <sup>4+</sup>	Ta <sup>5+</sup>	W <sup>6+</sup>

grows stronger ↑

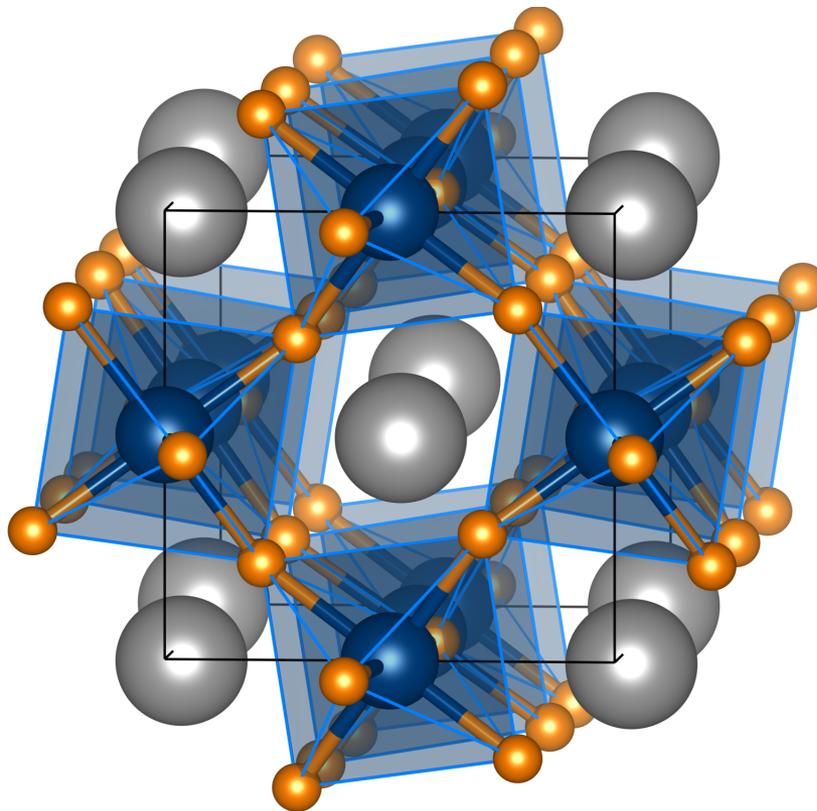
grows stronger →

Both JT and SOJT result in distortions, but the latter results in off-centering as well (*ie.* creates a local dipole).

Countercations (other cations) play a role in determining distortion:



*P4mm* BaTiO<sub>3</sub> at room temperature with distorted TiO<sub>6</sub> octahedra.



*Pnma* CaTiO<sub>3</sub> at room temperature with tilting and rotation, but relatively undistorted TiO<sub>6</sub> octahedra.

Cation centered lone pairs – the important cations (note the valence is 2 below the group valence):

	1+	2+	3+	4+	5+	6+
$3d^{10} 4s^2$	Ga	Ge	As	Se	Br	
$4d^{10} 5s^2$	In	Sn	Sb	Te	I	Xe
$5d^{10} 6s^2$	Tl	Pb	Bi	Po		

The sub-valent state is particularly important in the last row.

Hyde and Andersson, *Inorganic Crystal Structures*, Wiley (1988):

In many crystalline solids with cation-centered lone pairs, the lone pair occupies the same volume as an oxide or fluoride ion. However the cation-lone pair distances (in Å) is much shorter than typical cation-anion distances:

	1+	2+	3+	4+	5+	6+
3d <sup>10</sup> 4s <sup>2</sup>	Ga 0.95	Ge 1.05	As 1.26	Se 1.22	Br 1.47	
4d <sup>10</sup> 5s <sup>2</sup>	In 0.86	Sn 0.95	Sb 1.06	Te 1.25	I 1.23	Xe 1.49
5d <sup>10</sup> 6s <sup>2</sup>	Tl 0.69	Pb 0.86	Bi 0.98	Po 1.06		

*Polyhedra of anions and lone pairs must have off-centric cations.*

Cation-centered lone pairs (often with  $\text{Pb}^{2+}$  as the central cation, but also  $\text{Sn}^{2+}$  and  $\text{Bi}^{3+}$ ) are important for applications requiring off-centered polyhedra and their associated dipoles:

- Ferroelectric and piezoelectric materials, actuators
- High-refractive index materials (lead crystal)
- Ionic conductors
- Multiferroic materials
- Non-linear optical materials
- Phosphors
- Semiconductor/semimetal to insulator transitions

Visualization: DFT based on the Stuttgart TB-LMTO-ASA program  
 [O. K. Andersen, O. Jepsen etc.]

Electron localization functions (ELFs): An orbital independent measure of electron localization based on the pair probability of electrons [Becke, Edgecombe *J. Chem. Phys.* **92** (1990) 5397; Silvi, Savin, *Nature* **371** (1994) 683.]

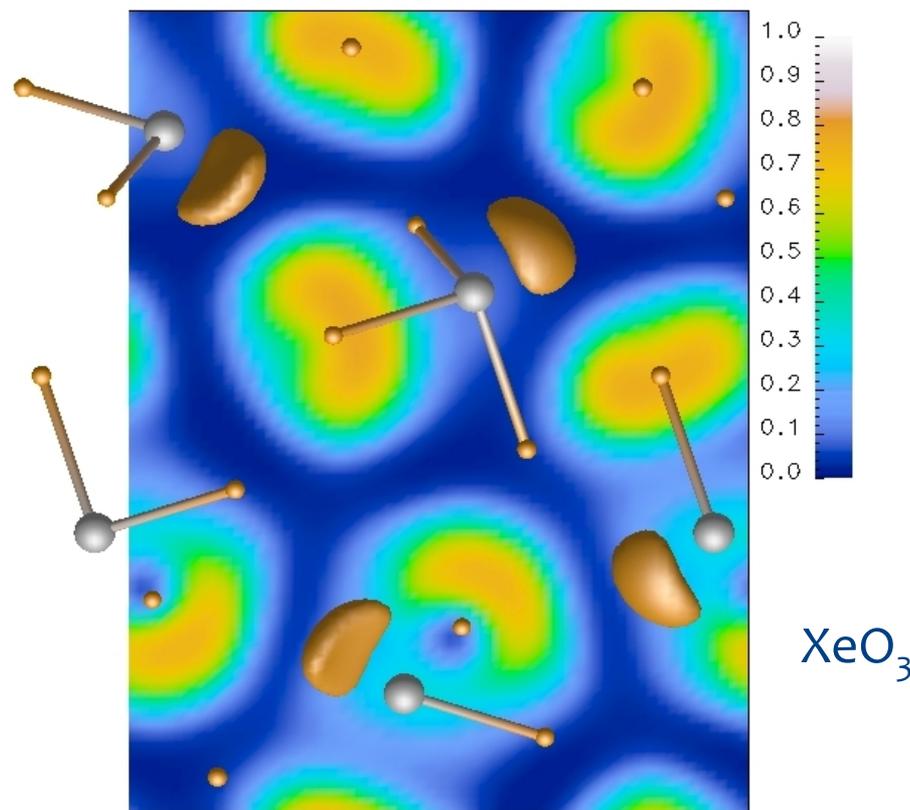
$$\text{ELF} = \frac{1}{1 + \left(\frac{D}{D_H}\right)^2} \in (0, 1)$$

with

$$D = \frac{1}{2} \sum_i |\nabla \phi_i|^2 - \frac{1}{8} \frac{|\nabla \rho|^2}{\rho}$$

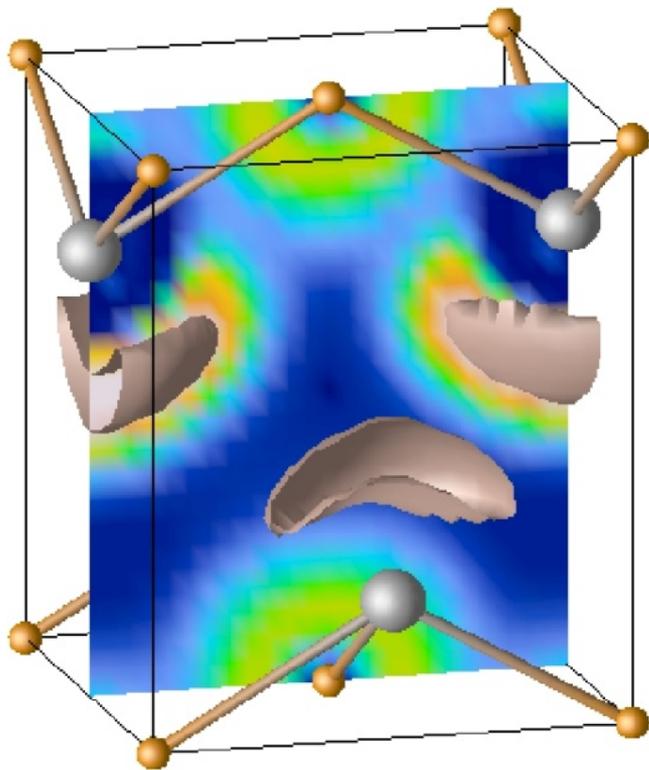
and

$$D_H = \frac{3}{10} (3\pi^2)^{5/3} \rho^{5/3}$$

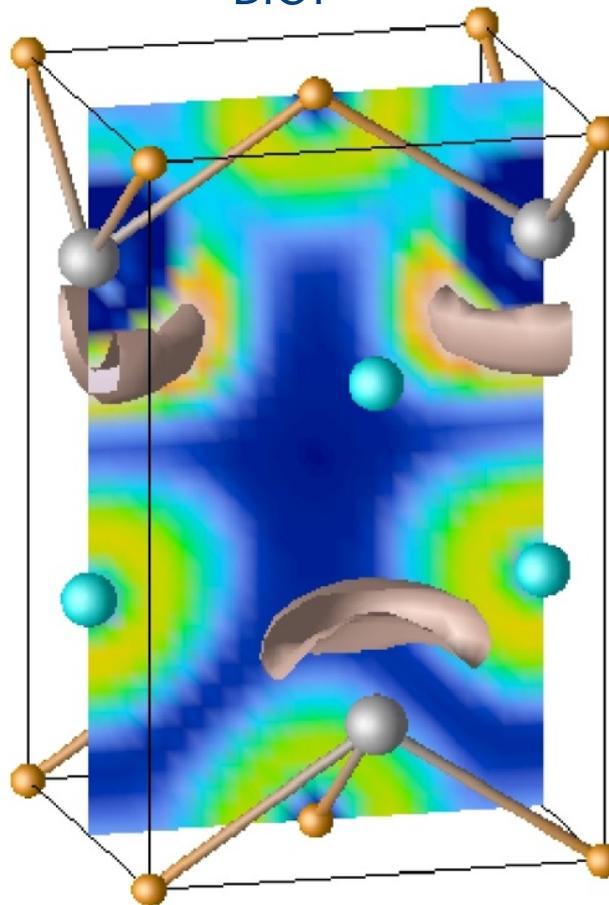


The electron density  $\rho$  does not reveal lone pairs.

$\alpha$ -PbO



BiOF

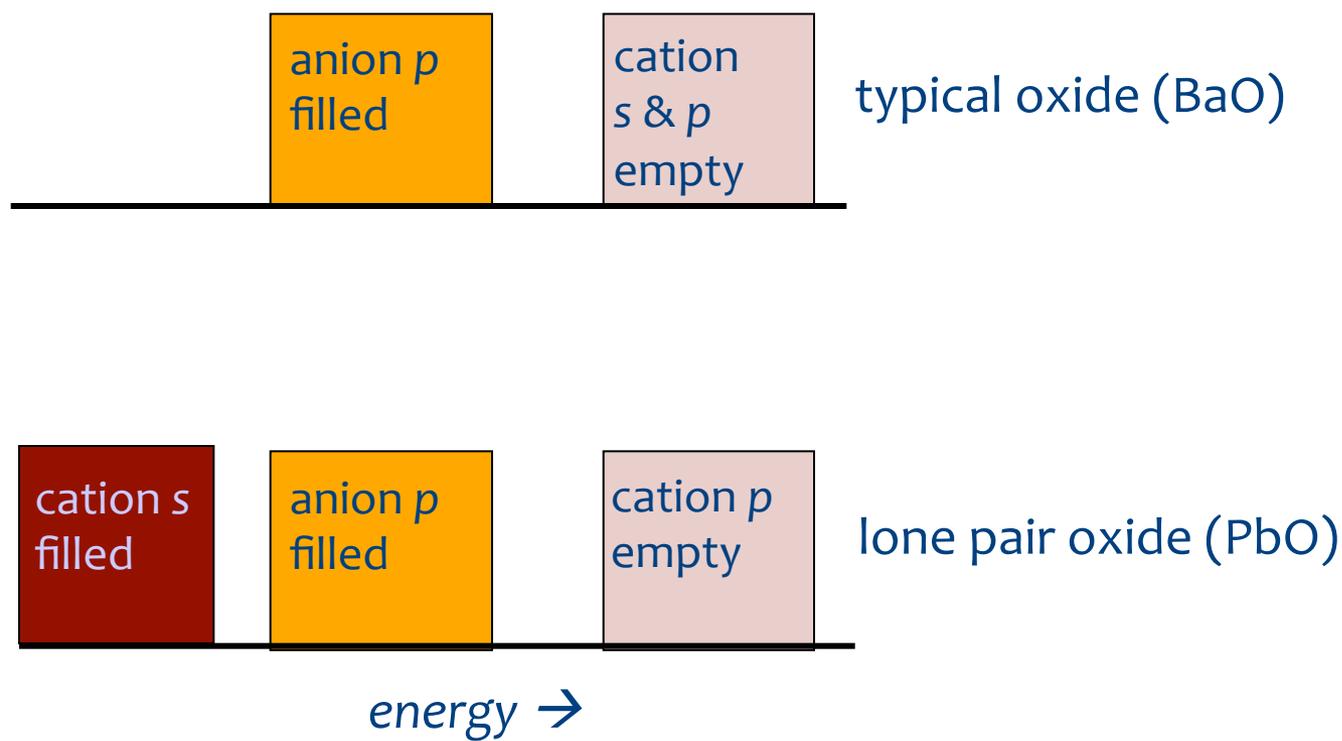


Lone pairs typically visualized with ELF values between 0.65 and 0.9

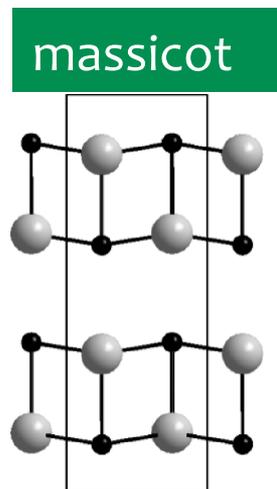
## Composition of the lone pair

Orgel (1959): The lone pair cannot have purely s character when it is stereochemically active; it must admix with p.

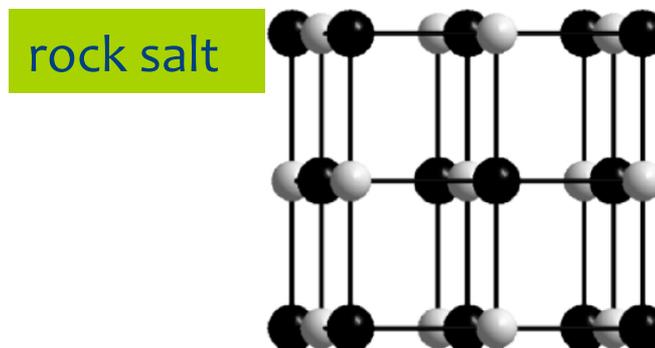
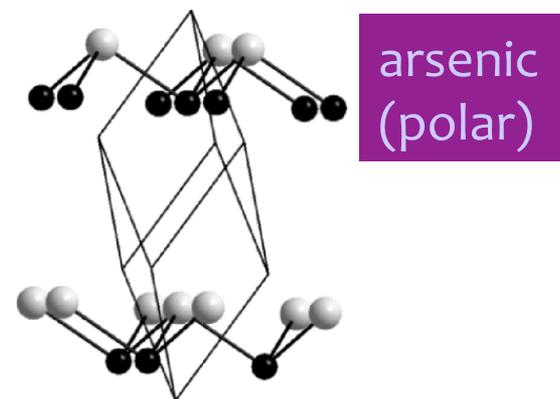
Bersuker (1984): Filled anion p states must play a role.

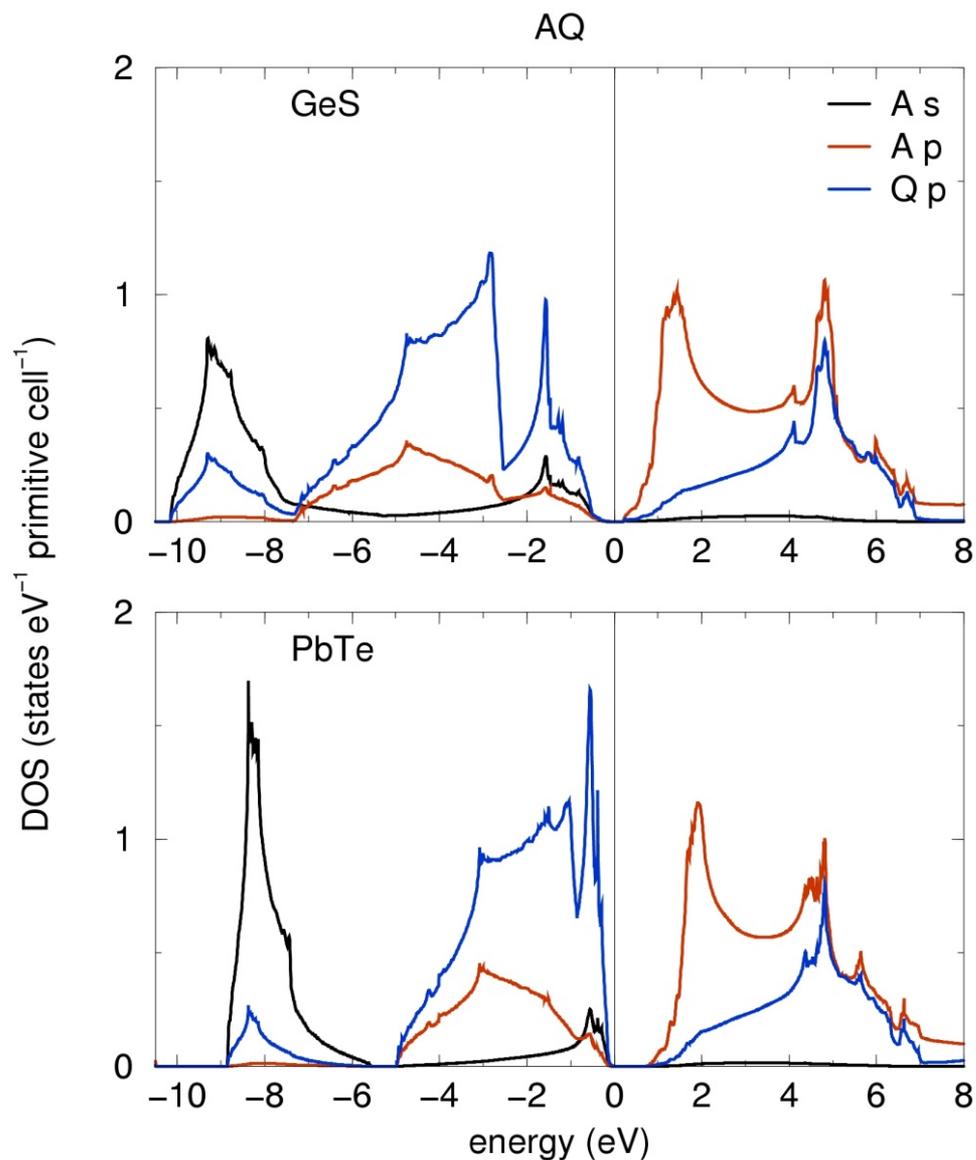


A lone pair sorted structural field AQ (IV-VI semiconductors): The lone pair is not always active!



	S	Se	Te
Ge	GeS	GeSe	GeTe
Sn	SnS	SnSe	SnTe
Pb	PbS	PbSe	PbTe



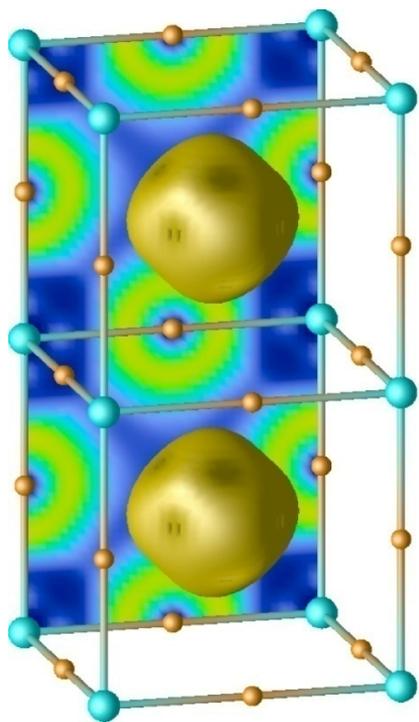


	S	Se	Te
Ge	GeS	GeSe	GeTe
Sn	SnS	SnSe	SnTe
Pb	PbS	PbSe	PbTe

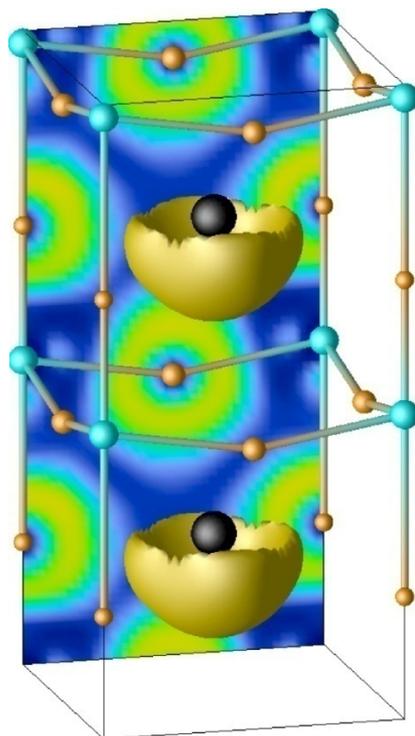
When the lone pair is stereochemically active (as in GeS), cation *s* states are broader and are better mixed with anion *p* states. The mixing is intermediated by empty cation *p*.

Cation *s* states are narrow and largely unmixed with anion *p* in cases when the lone pair is not stereochemically active (cf. the inert pair effect).

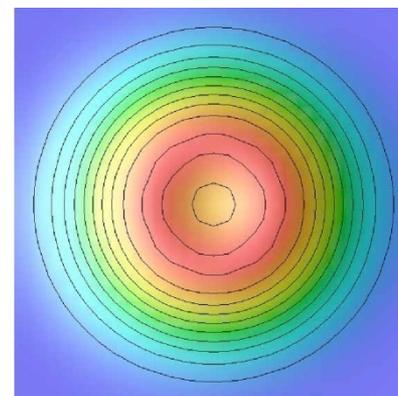
The expression of cooperative stereochemical activity of the lone pair plays an important role in the development of polar behavior.



$\text{PbTiO}_3$  above  
766 K  
 $Pm-3m$



$\text{PbTiO}_3$  below  
766 K  
 $P4mm$



Even above the phase transition, the  $\text{Pb}^{2+}$  ion (here, in  $\text{Pb}_2\text{NbYbO}_6$ ) is not really where it is supposed to be.

Baldinozzi, Raulot, Seshadri, *MRS Symp. Proc.* **718** (2002) D12.7.1.



Thank you